

Health-check of supersymmetric $E(6)$ models into the new decade

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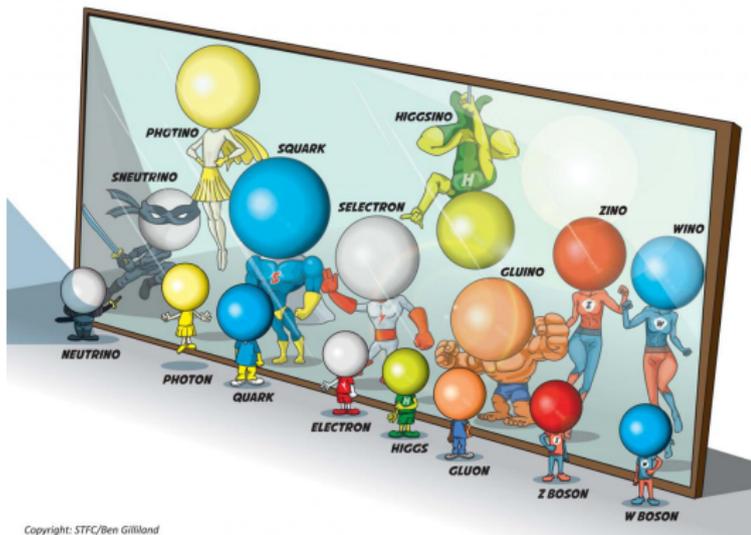
Talk based on M.Frank, Y. Hiçyılmaz, S. Moretti and Ö. Özdal
“ E_6 Motivated UMSSM Confronts Experimental Data” hep-ph/2004.01415

NExT Institute Spring Workshop 2020
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Outline

- 1 Introduction
 - Supersymmetry
 - Cons of MSSM
- 2 E_6 Motivated UMSSM
 - Model
 - Scanning Procedure and Experimental Constraints
- 3 Results
- 4 Conclusion

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 - The Hierarchy Problem.
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 - WIMP candidate in order to solve the DM puzzle.
- Minimal Supersymmetric Standard Model (MSSM) is the simplest SUSY extension of the SM.

$$W_{MSSM} = \mu H_u H_d + Y_u \hat{Q} H_u \hat{U} + Y_d \hat{Q} H_d \hat{D} + Y_e \hat{L} H_d \hat{E}$$

Little Hierarchy Problem!!!

$$(m_h^{pole})^2 \approx m_Z^2 \cos^2 2\beta + \Delta m_h^2$$

$$m_h^{pole} \approx 125 \text{ GeV}$$

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$$\Delta m_h \gtrsim 87 \text{ GeV}$$

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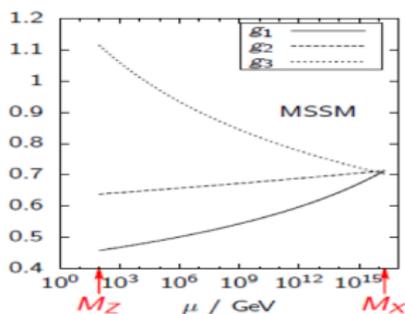
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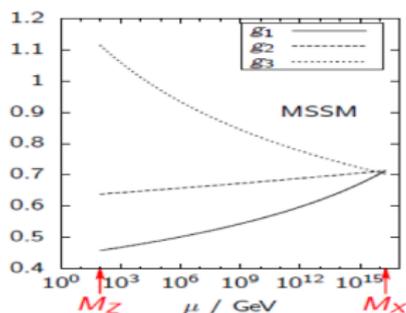
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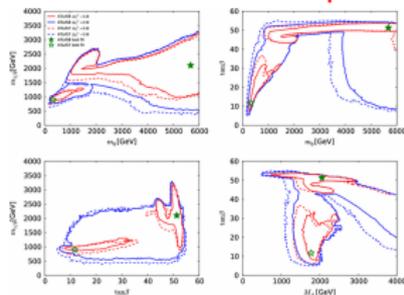
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Excluded Parameter Space!!!



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- These models can dynamically generate the μ term at the EW scale.
- One of them is the scenario which can be realised by breaking the exceptional group E_6 , so called E_6 motivated UMSSM.
 - The fundamental 27-dimensional representations.
 - Cancellation of gauge anomalies.
 - See-saw mechanisms for neutrino mass and mixing generation.

$$E_6 \rightarrow SO(10) \times U(1)_{\psi} \rightarrow SU(5) \times U(1)_{\chi} \times U(1)_{\psi} \rightarrow G_{\text{MSSM}} \times U(1)'$$
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Superpotential:

$$W_{\text{UMSSM}} = Y_u \hat{Q} H_u \hat{U} + Y_d \hat{Q} H_d \hat{D} + Y_e \hat{L} H_d \hat{E} + h_s S H_d H_u$$

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U(1)' Charges:

Model	\hat{Q}	\hat{U}^c	\hat{D}^c	\hat{L}	\hat{E}^c	\hat{H}_d	\hat{H}_u	\hat{S}
$2\sqrt{6} U(1)_\psi$	1	1	1	1	1	-2	-2	4
$2\sqrt{10} U(1)_\chi$	-1	-1	3	3	-1	-2	2	0

$$Q^i = Q_\chi^i \cos \theta_{E_6} - Q_\psi^i \sin \theta_{E_6}$$

Higgs Potential:

$$\begin{aligned}
 V_{Higgs}^{UMSSM} &= V_{Higgs}^{MSSM} |_{\mu=h_S S} + m_S^2 |S|^2 \\
 &+ \frac{g'^2}{2} (Q_{H_u} |H_u|^2 + Q_{H_d} |H_d|^2 + Q_S |S|^2)
 \end{aligned}$$

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Z-Z' Mass Mixing:

$$\mathbf{M}_Z^2 = \begin{pmatrix} M_{ZZ}^2 & M_{ZZ'}^2 \\ M_{ZZ'}^2 & M_{Z'Z'}^2 \end{pmatrix} = \begin{pmatrix} 2g_1^2 \sum_i t_{3i}^2 |\langle \phi_i \rangle|^2 & 2g_1 g' \sum_i t_{3i} Q_i |\langle \phi_i \rangle|^2 \\ 2g_1 g' \sum_i t_{3i} Q_i |\langle \phi_i \rangle|^2 & 2g'^2 \sum_i Q_i^2 |\langle \phi_i \rangle|^2 \end{pmatrix}$$

$$\tan 2\alpha_{ZZ'} = \frac{2M_{ZZ'}^2}{M_{Z'Z'}^2 - M_{ZZ}^2}.$$

$$M_{Z,Z'}^2 = \frac{1}{2} \left[M_{ZZ}^2 + M_{Z'Z'}^2 \mp \sqrt{(M_{ZZ}^2 - M_{Z'Z'}^2)^2 + 4M_{ZZ'}^4} \right].$$

Kinetic Mixing:

$$\mathcal{L}_{\text{kin}} \supset -\frac{\kappa}{2} \hat{B}^{\mu\nu} \hat{Z}'_{\mu\nu}$$

$$\begin{pmatrix} \hat{B}_\mu \\ \hat{Z}'_\mu \end{pmatrix} = \begin{pmatrix} 1 & -\frac{\kappa}{\sqrt{1-\kappa^2}} \\ 0 & \frac{1}{\sqrt{1-\kappa^2}} \end{pmatrix} \begin{pmatrix} B_\mu \\ Z'_\mu \end{pmatrix}$$

$$g_y = \frac{g_{YY}g_{EE} - g_{YE}g_{EY}}{\sqrt{g_{EE}^2 + g_{EY}^2}} = g_1,$$

$$g_{yp} = \frac{g_{YY}g_{EY} + g_{YE}g_{EE}}{\sqrt{g_{EE}^2 + g_{EY}^2}} = \frac{-\kappa g_1}{\sqrt{1-\kappa^2}},$$

$$g_p = \frac{g'}{\sqrt{1-\kappa^2}}$$

$$G = \begin{pmatrix} g_{YY} & g_{YE} \\ g_{EY} & g_{EE} \end{pmatrix}$$

Kinetic Mixing:

$$\mathcal{L}_{\text{int}} = -\bar{\psi}_i \gamma^\mu \left[g_y Y_i B_\mu + (g_p Q_i + g_{yp} Y_i) Z'_\mu \right] \psi_i$$

$$Q_i^{\text{eff}} = Q_i - \kappa \frac{g_1}{g'} Y_i$$

Parameter Space

Parameter	Scanned range	Parameter	Scanned range
m_0	[0., 3.] TeV	h_s	[0., 0.7]
$M_{1,4}/M_3$	[-15., 15.]	ν_S	[1., 15.] TeV
M_3	[0., 3.] TeV	A_s	[-5., 5.] TeV
M_2/M_3	[-5., 5.]	θ_{E_6}	$[-\pi/2, \pi/2]$
$\tan \beta$	[1., 50.]	κ	[-0.5, 0.5]
A_0	[-5., -5.] TeV		

Constraints

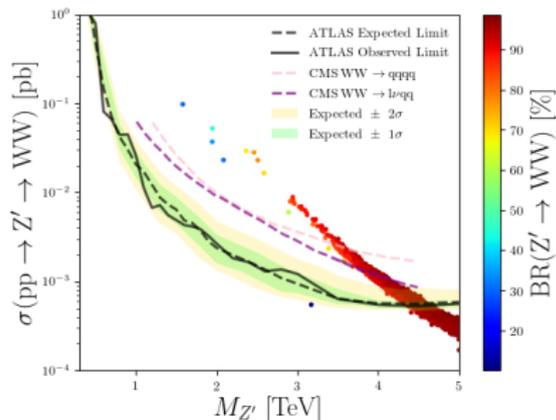
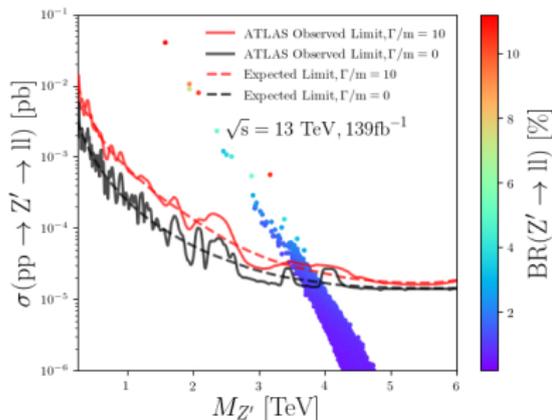
$$\begin{aligned} m_h &= 123 - 127 \text{ GeV (and SM - like couplings)}, \\ m_{\tilde{g}} &\geq 1.8 \text{ TeV}, \\ 0.8 \times 10^{-9} &\leq \text{BR}(B_s \rightarrow \mu^+ \mu^-) \leq 6.2 \times 10^{-9} \text{ (} 2\sigma \text{ tolerance)}, \\ m_{\tilde{\chi}_1^0} &\geq 103.5 \text{ GeV}, \\ m_{\tilde{\tau}} &\geq 105 \text{ GeV}, \\ 2.99 \times 10^{-4} &\leq \text{BR}(B \rightarrow X_s \gamma) \leq 3.87 \times 10^{-4} \text{ (} 2\sigma \text{ tolerance)}, \\ 0.15 &\leq \frac{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{UMSSM}}}{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{SM}}} \leq 2.41 \text{ (} 3\sigma \text{ tolerance)}, \\ 0.0913 &\leq \Omega_{\text{CDM}} h^2 \leq 0.1363 \text{ (} 5\sigma \text{ tolerance)}. \end{aligned} \tag{1}$$

Colour Coding

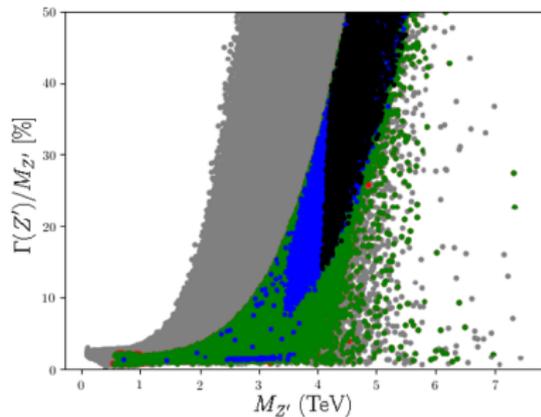
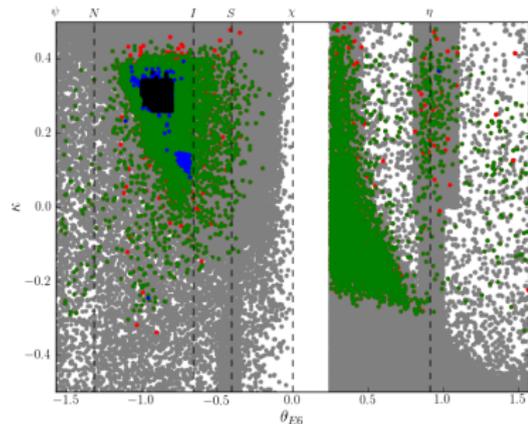
- Grey: Radiative EWSB (REWSB) and neutralino LSP.
- Red: The subset of grey plus Higgs boson mass and coupling constraints, SUSY particle mass bounds and EWPT requirements.
- Green: The subset of red plus B -physics constraints.
- Blue: The subset of green plus WMAP constraints on the relic abundance of the neutralino LSP (within 5σ).
- Black: The subset of blue plus exclusion limits at the LHC from Z' direct searches via $pp \rightarrow Z' \rightarrow ll$ and $pp \rightarrow Z' \rightarrow WW$.

Z' Mass Limits

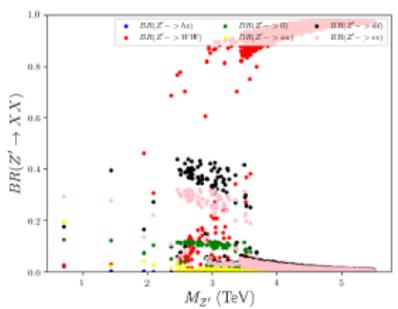
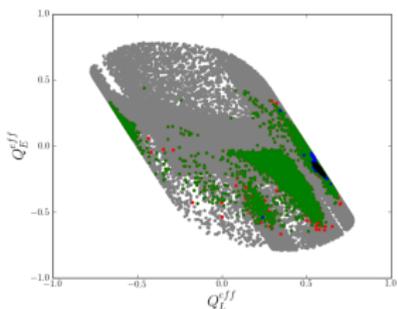
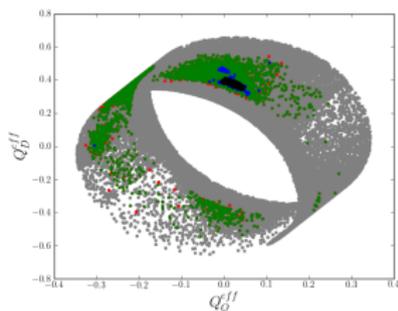
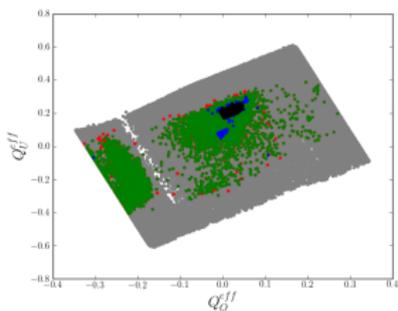
$\Gamma(Z' \rightarrow WW)$ is proportional to $M_{Z'}^5/M_W^4$ as well as $\sin^2 \alpha_{ZZ'}$.



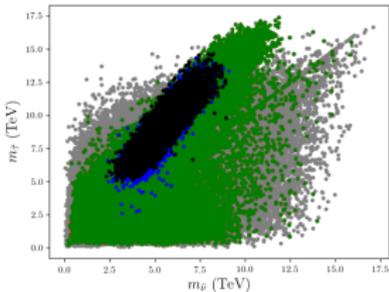
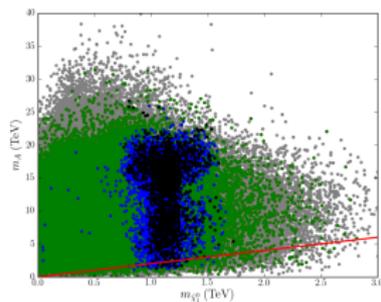
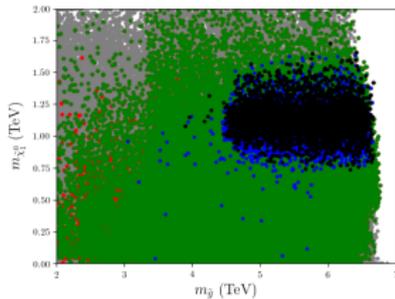
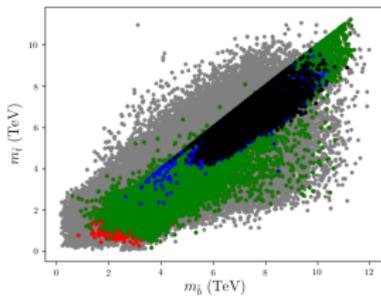
Parameter Space and Z' Decay Width



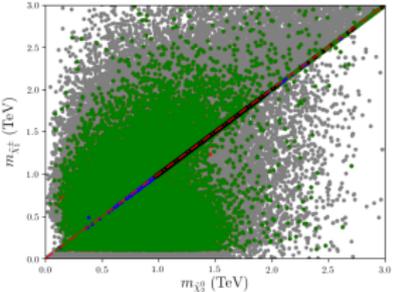
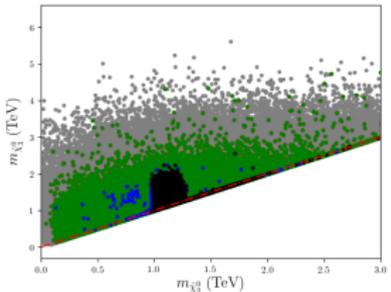
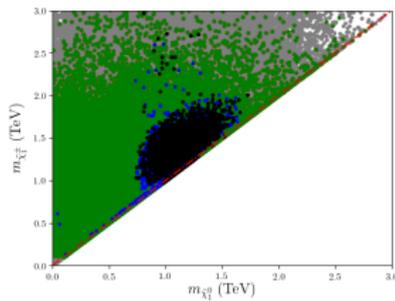
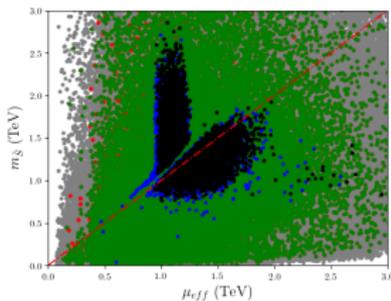
Effective $U(1)'$ Charges and Z' Decays



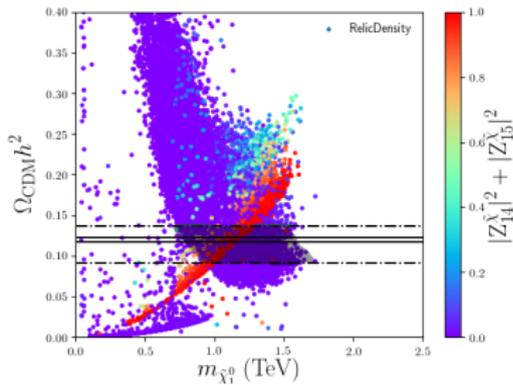
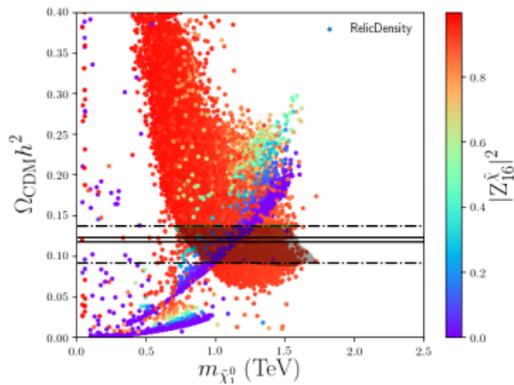
SUSY Mass Spectrum



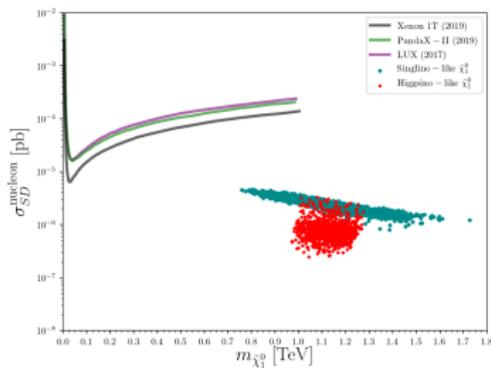
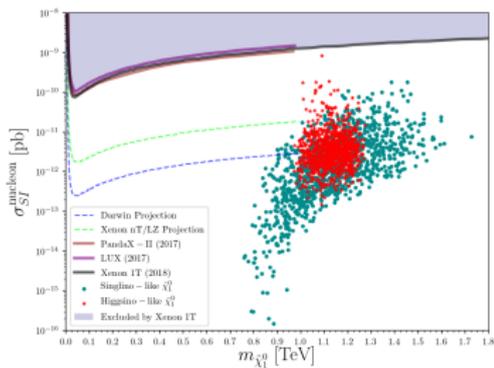
Neutralino Masses



Dark Matter-Relic Density



Dark Matter-Direct Detection



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- The fundamental parameters, i.e., the gauge kinetic mixing coefficient and the E_6 mixing angle, are found to be $0.2 \lesssim \kappa \lesssim 0.4$ and $-1 \lesssim \theta_{E6} \lesssim -0.8$ radians.

- We have found two specific Dark Matter LSP compositions which are consistent with all current experimental bounds coming from relic density and direct detection experiments : a higgsino-like LSP neutralino with $0.9 \text{ TeV} \lesssim m_{\chi_1^0} \lesssim 1.2 \text{ TeV}$ and a singlino-like LSP neutralino with $0.9 \text{ TeV} \lesssim m_{\chi_1^0} \lesssim 1.6 \text{ TeV}$.

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- Our solutions which are compatible with experimental bounds include heavy sparticle spectrum for third generation sfermions ($m_{\tilde{t}, \tilde{b}} \gtrsim 4 \text{ TeV}$ and $m_{\tilde{\tau}} \gtrsim 5 \text{ TeV}$) as well as the gluino ($m_{\tilde{g}} \gtrsim 4 \text{ TeV}$).

Thank You for Your Attention!!!