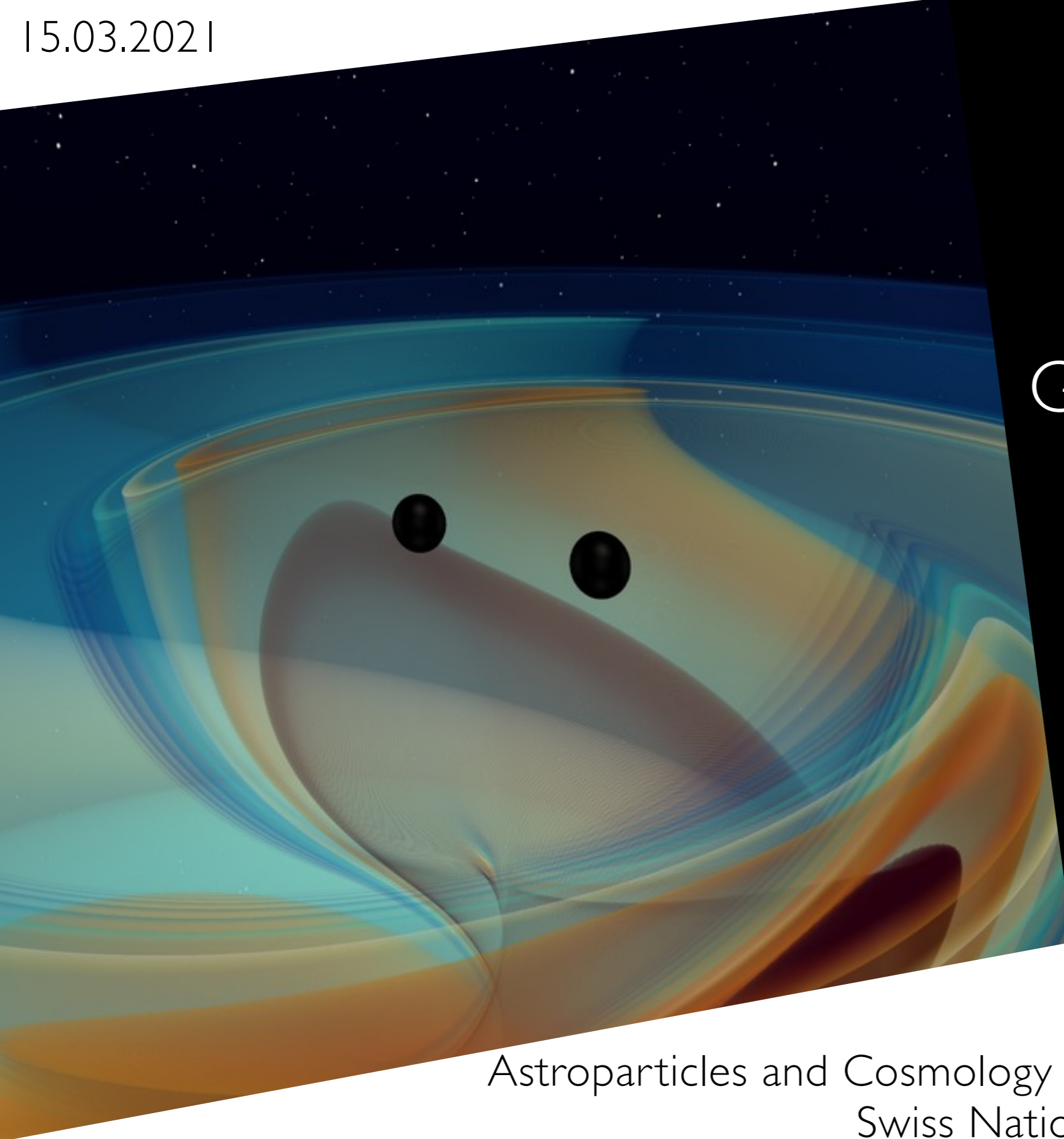


King's College London - EPAP Seminar

15.03.2021



Enhancing Gravitational-Wave Science with Machine Learning

Leila Haegel

Astroparticles and Cosmology Laboratory, University of Paris
Swiss National Science Foundation fellow

▶ **GW physics**

- A primer on GW astrophysics
- Ground-based interferometers
- Detection and analysis
- Examples of physics results

▶ **Machine learning applications**

- Why ML?
- Characterisation of detector noise
- Detection of astrophysical signals
- GW modelling
- Estimation of the GW sources parameters

GW physics

- **A primer on GW astrophysics**
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Gravitational waves primer 1/2

- ▶ **A prediction from GR:** linearised Einstein Equation for accelerating masses:

$$G_{\mu\nu} = 8\pi T_{\mu\nu} \quad \rightarrow \quad \left(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2} \right) T_{\mu\nu} = 0$$

- ▶ **Propagation:** GW modify the spacetime according to:

$$ds^2 = \underbrace{-c dt^2}_{\text{propagate at speed of light}} + \underbrace{[1 - h(z \pm ct)] dx^2}_{\text{GW deformation}} + \underbrace{[1 - h(z \pm ct)] dy^2}_{\text{GW deformation}} + \underbrace{dz^2}_{\text{transverse waves}}$$

- ▶ **Radiation mode:** GW are tensor perturbation, the spacetime stretch is quadrupolar

Energy conservation \leftrightarrow no monopole radiation
Momentum conservation \leftrightarrow no dipole radiation

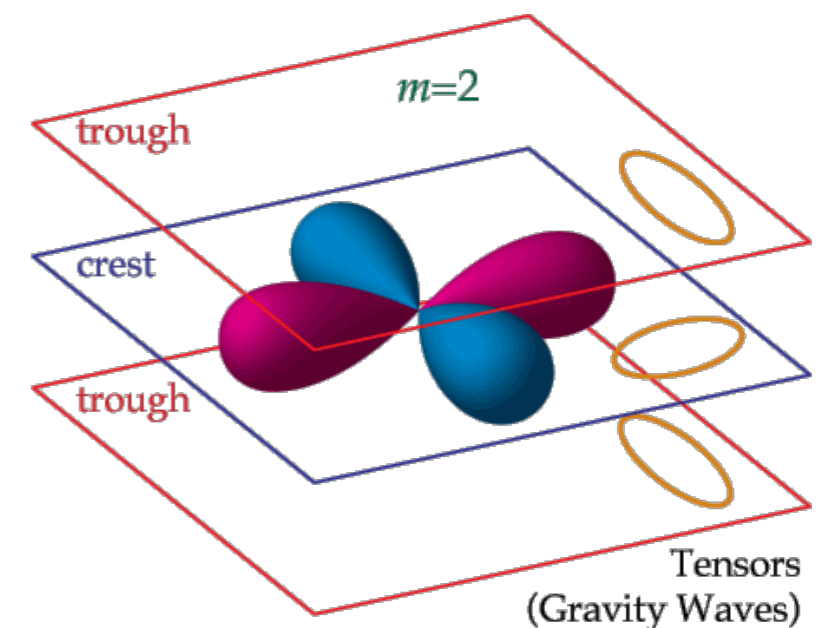


Image by Wayne Hu

Gravitational waves primer 2/2

- ▶ **Polarisations:** GW have 2 polarisations, h_+ and h_\times

- ▶ **Strain:** is the fractional change in distance between two points when a GW passes through:
$$\frac{\Delta L}{L} = \frac{1}{2} h_{xx}(0, ct)$$

- ▶ **Deformation:**

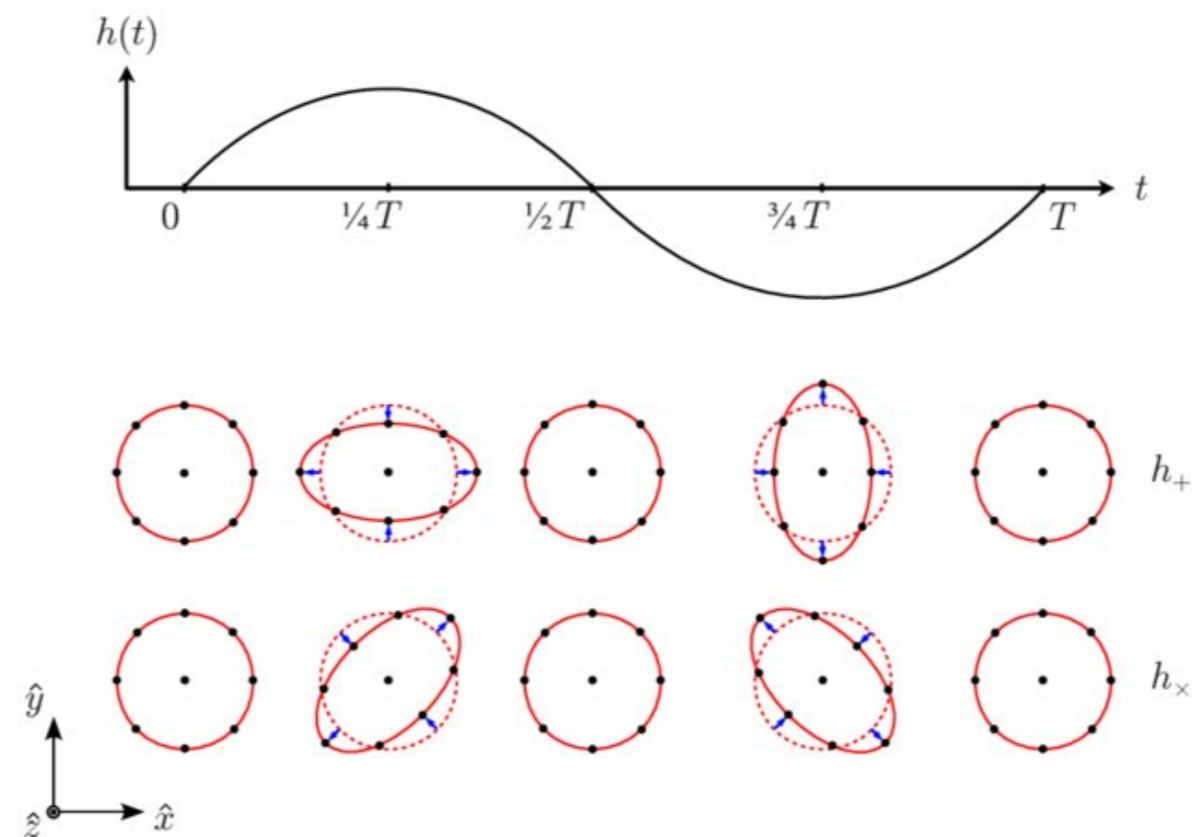


Figure by Alexandre Le Tiec

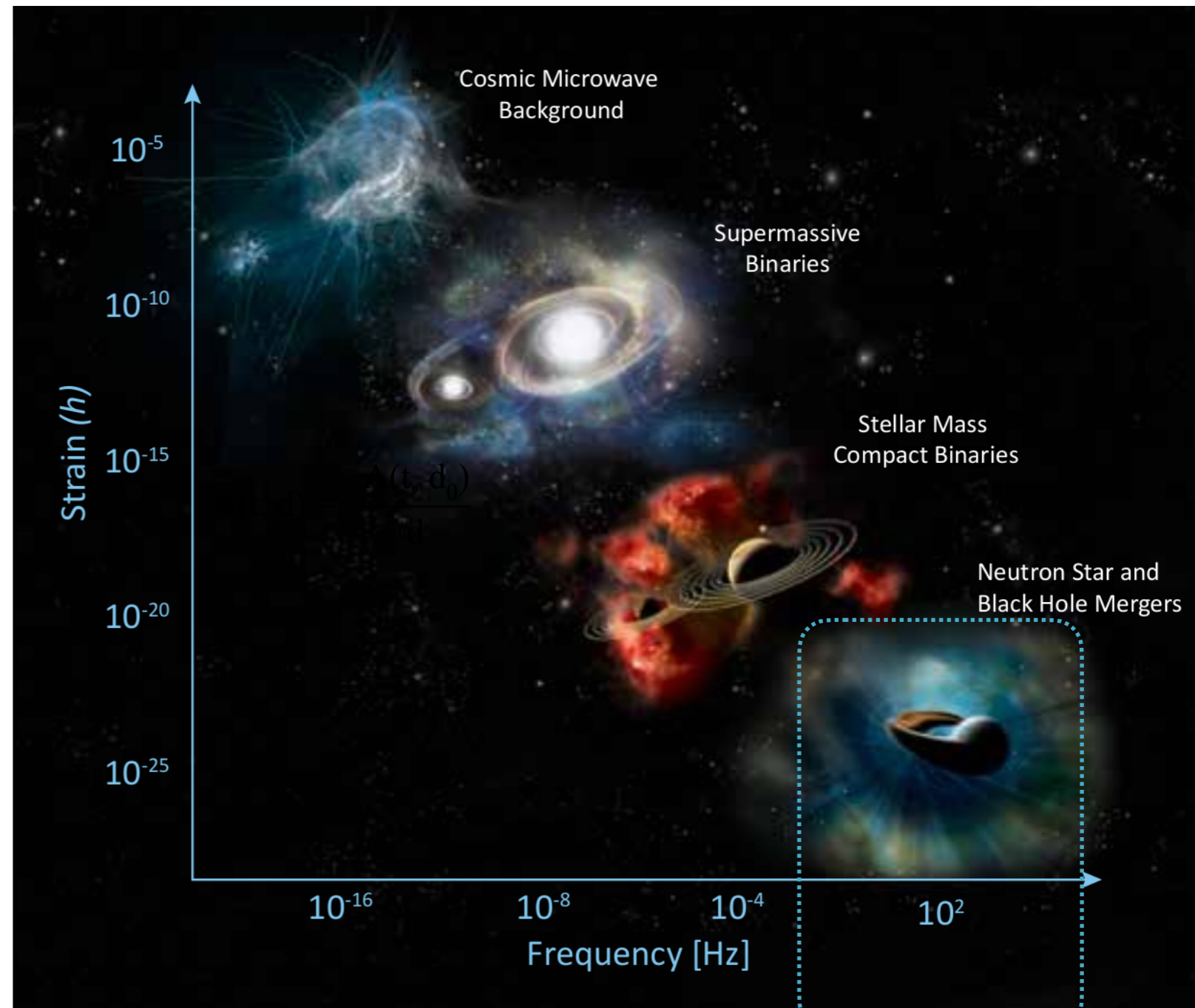
Gravitational waves sources

- ▶ **Strain:** follows a wave equation:

$$h(t) = A(t) \sin(\omega(t) t)$$

- ▶ **Amplitude:** decreases from the source as the GW propagates in spacetime

Credit: SSU EPO/Aurore Simonnet



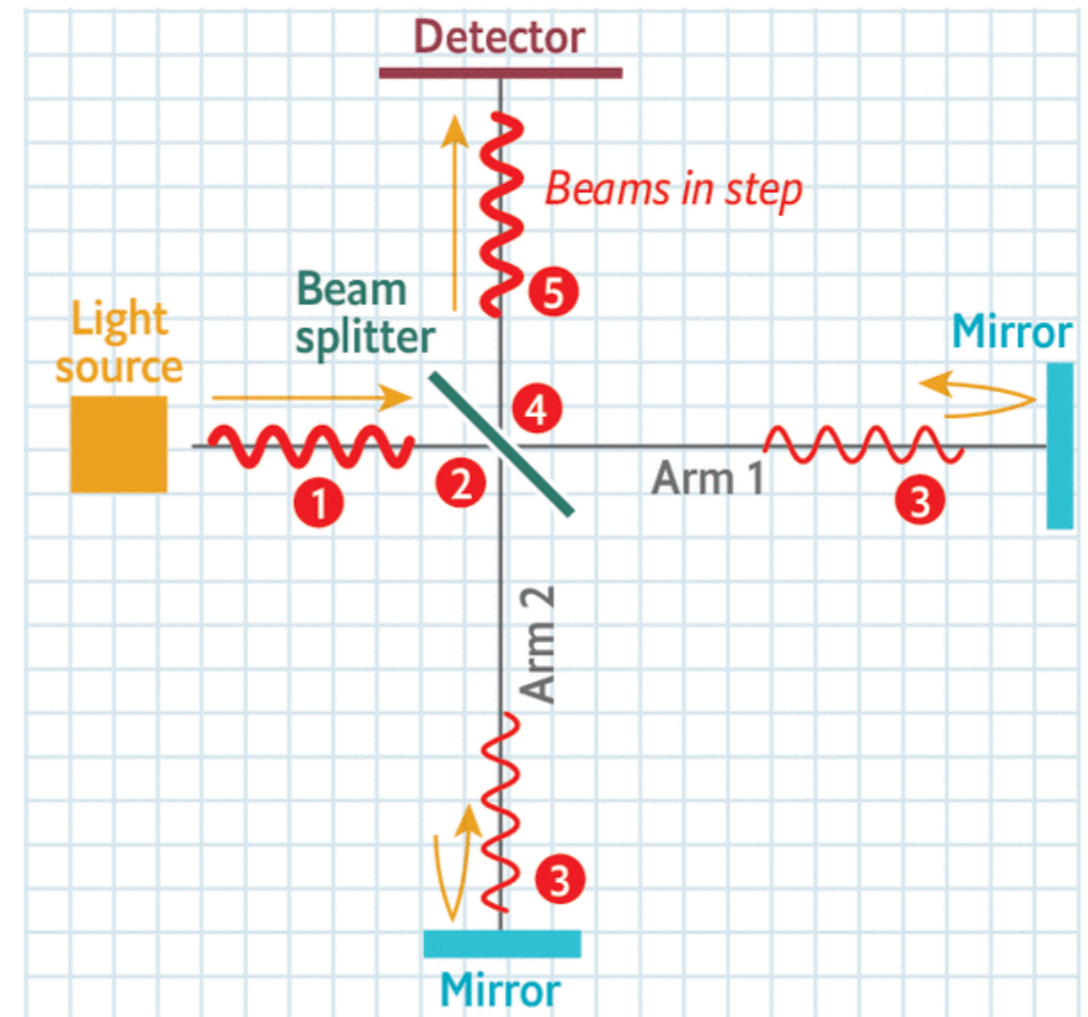
LIGO-Virgo-KAGRA

GW physics

- A primer on GW astrophysics
- **Ground-based interferometers**
- Detection and analysis
- Examples of physics results

Gravitational waves detection

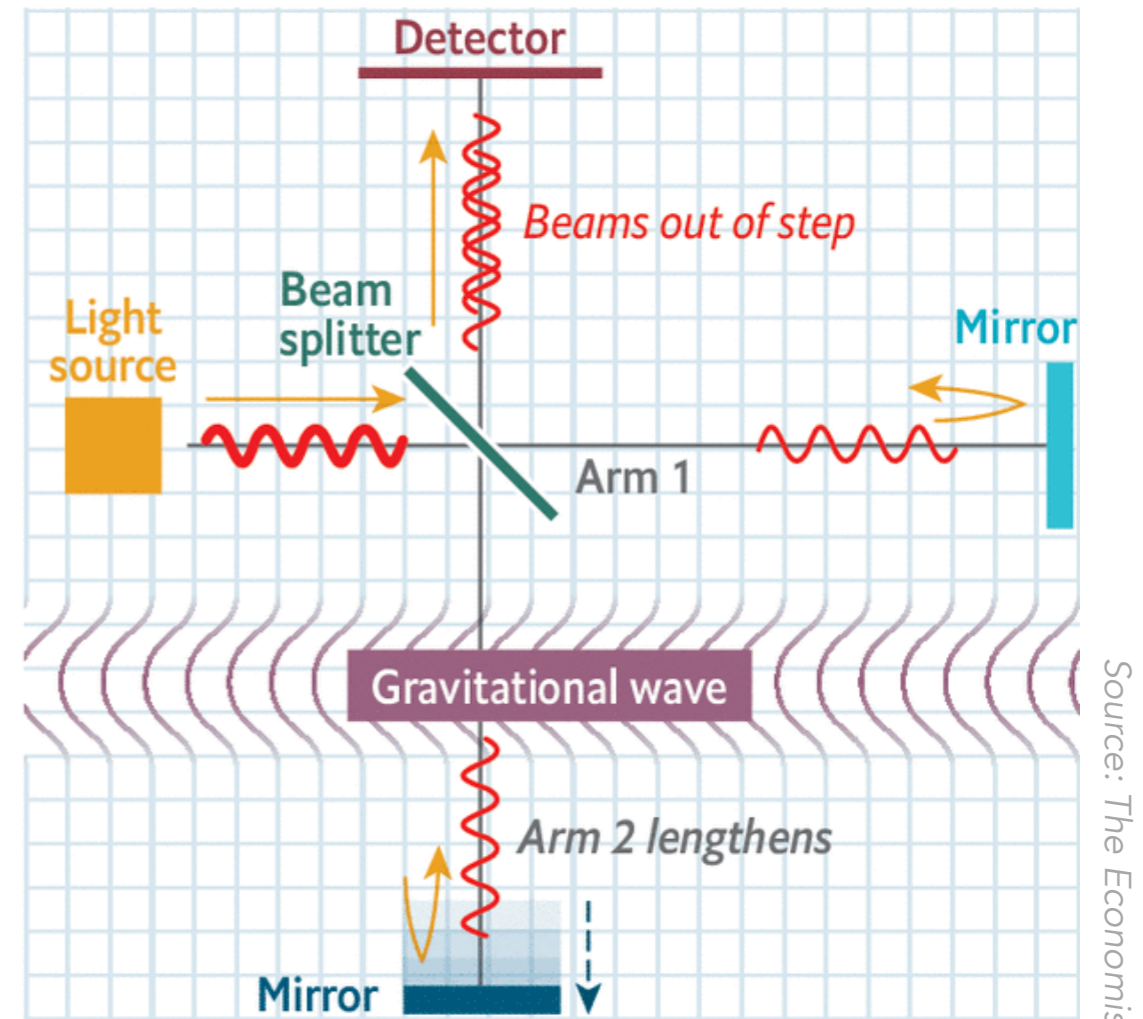
- ▶ The variation of space-time interval is measured with **light interferometry**.
- ▶ A light beam is divided in **two beams** travelling along orthogonal arms.
- ▶ Mirrors in the end of the arms reflect the beams back to a **photodetector**.
- ▶ If no gravitational wave passes through, the arm length remains the same and **the interference pattern is the sum of the splitted electromagnetic waves**.



Source: The Economist

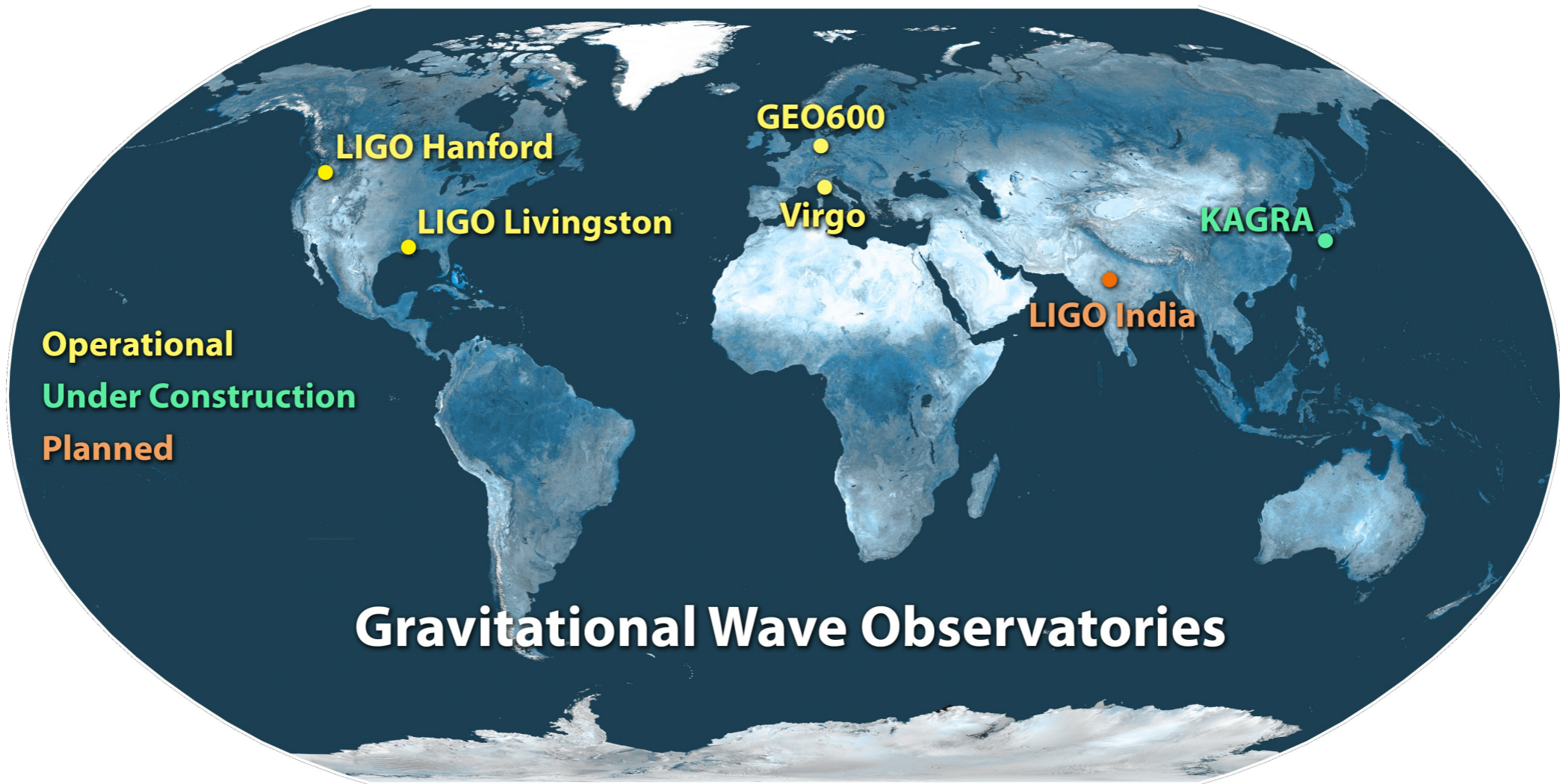
Gravitational waves detection

- ▶ The variation of space-time interval is measured with **light interferometry**.
- ▶ A light beam is divided in **two beams** travelling along orthogonal arms.
- ▶ Mirrors in the end of the arms reflect the beams back to a **photodetector**.
- ▶ If a gravitational wave passes through, the arm length is different and **the interference pattern is distorted**.

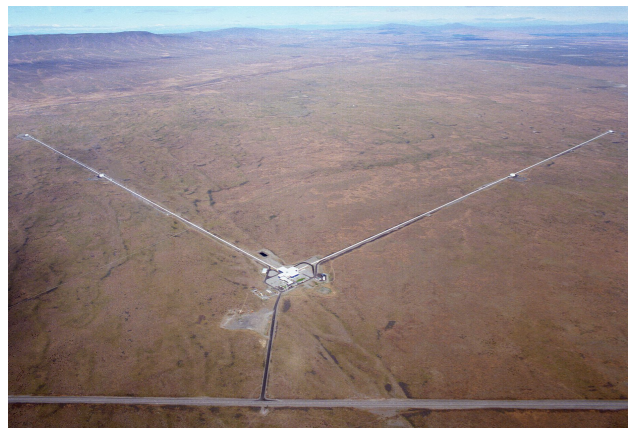


Source: The Economist

Gravitational waves observatories



LIGO Hanford



LIGO Livingston



Virgo

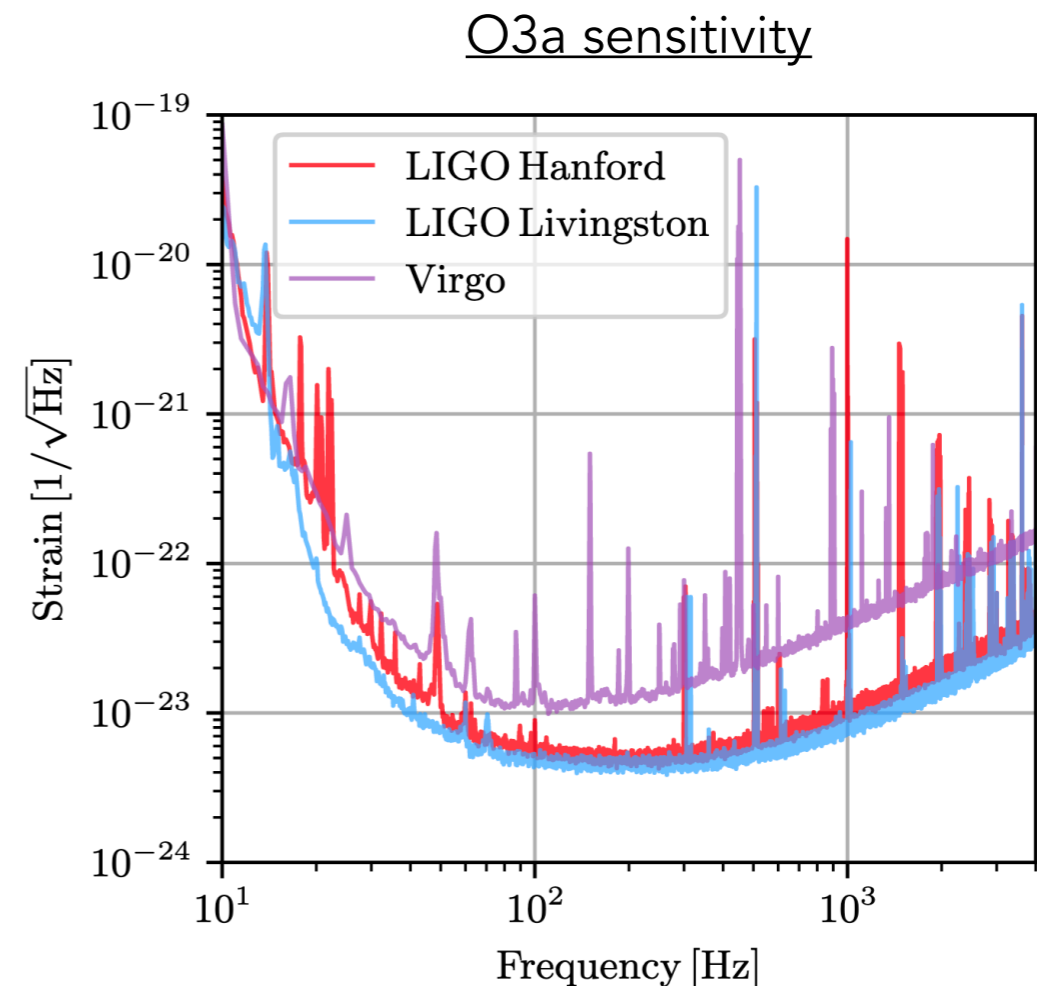
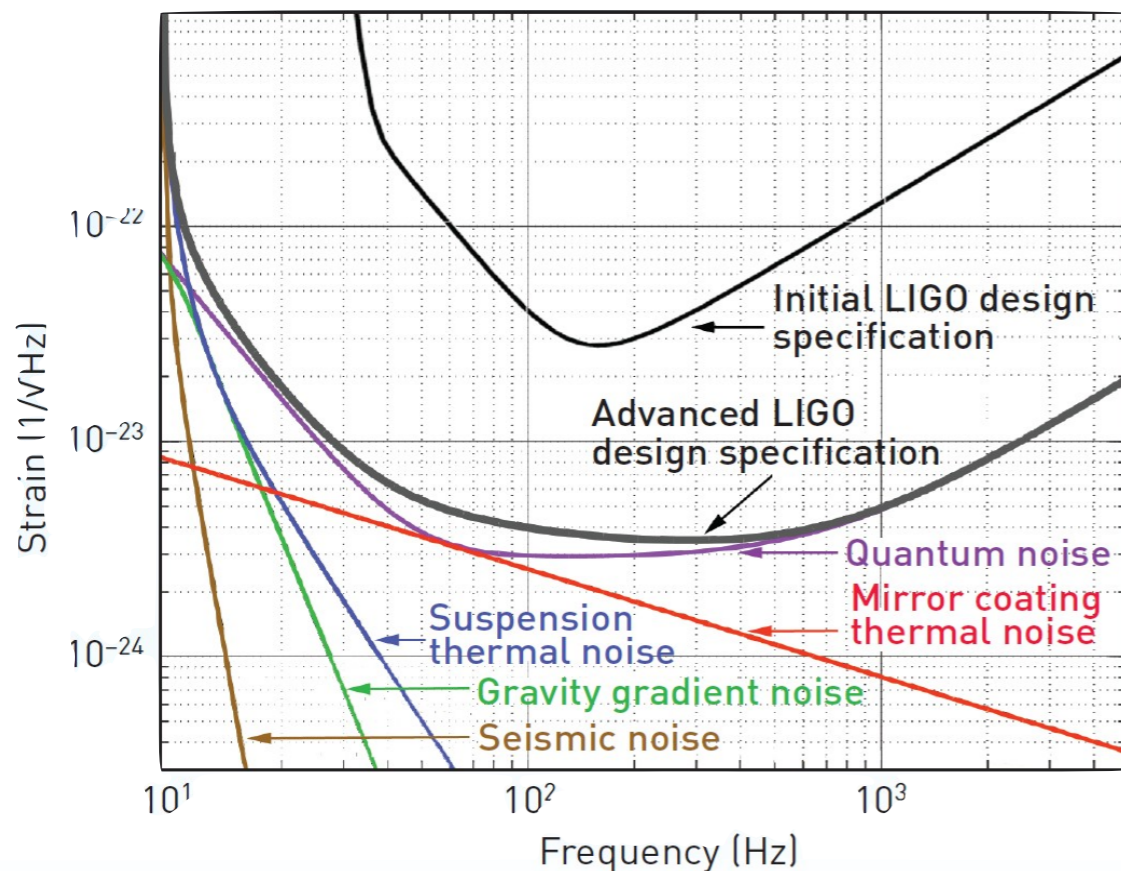


KAGRA



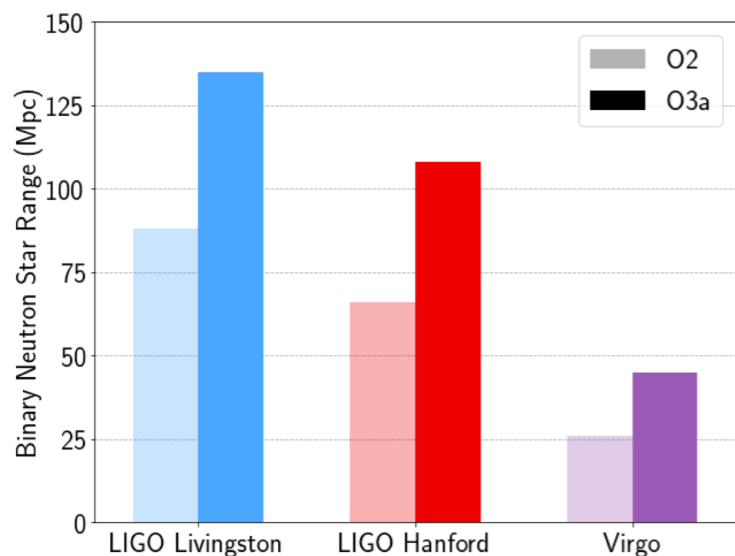
LIGO-Virgo sensitivities

- ▶ Ground-based light interferometers are sensitive to the **frequency range 10 - 10³ Hz**
- ▶ Signals entering the detection range are **coalescence of compact binaries** (stellar-mass black holes or neutron stars) and possibly pulsars



GW physics

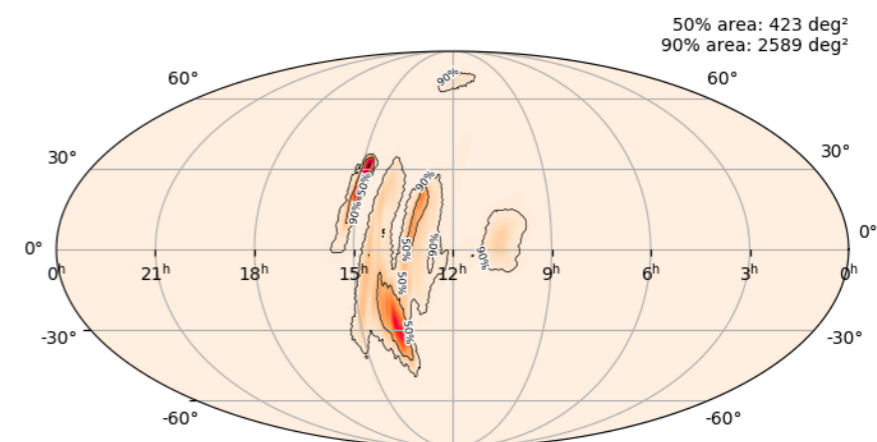
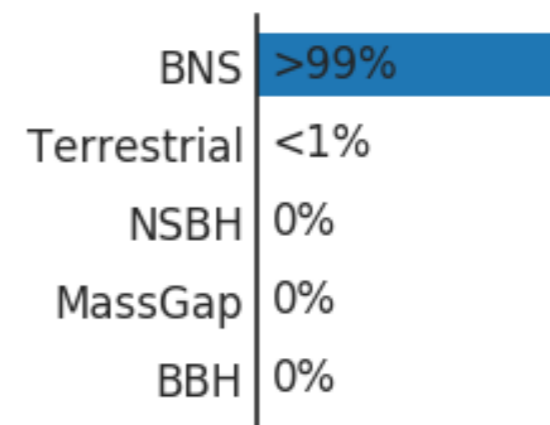
- A primer on GW astrophysics
- Ground-based interferometers
- **Detection and analysis**
- Examples of physics results



Credit: LIGO-Virgo Collaboration / Eve Chase / Caitlin Rose / Northwestern / University of Wisconsin-Milwaukee

- ▶ **Detection range:** during O3 run
- ▶ **Different type of searches:**
 - 4 modelled searches pipelines
 - 2 unmodelled searches pipelines

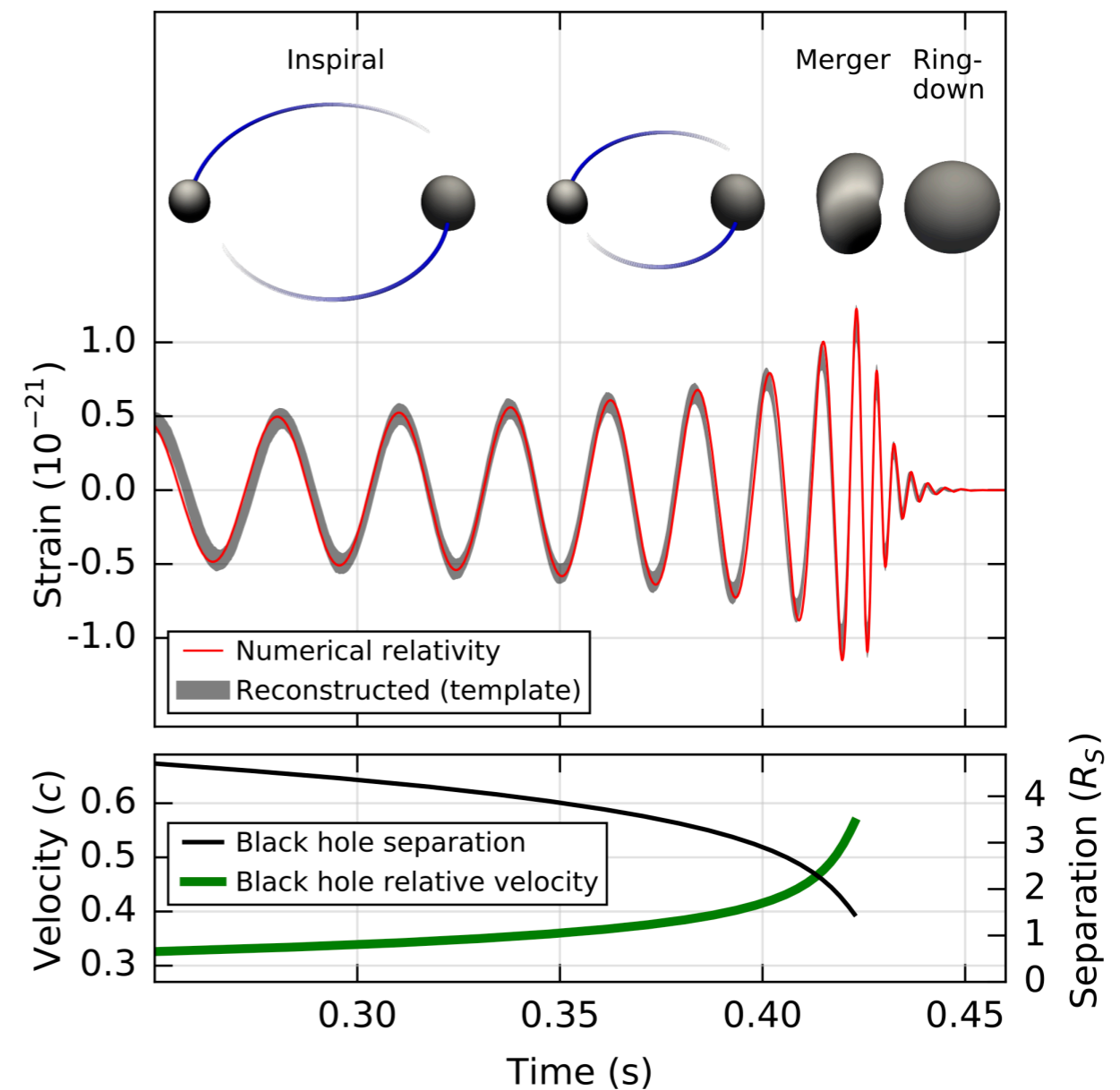
- ▶ **Database automatically updated:**
 - GraceDB contains low-latency information about the event
 - In case of possible neutron star, alert sent to satellites and telescopes to search for electromagnetic counterpart



GW signals from binary systems of compact objects

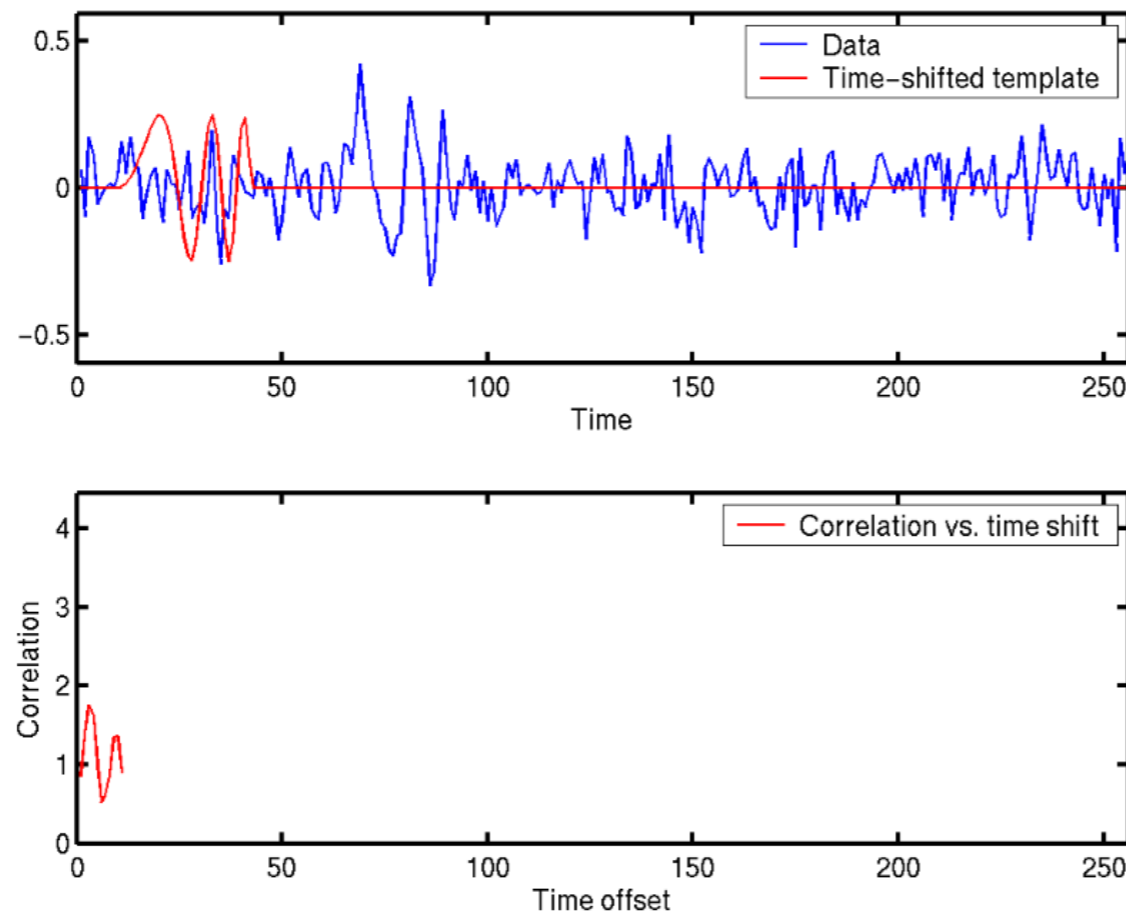
- ▶ **Black holes / neutron stars** orbiting in binaries emit gravitational waves.
- ▶ When the distance between the objects is large, the **inspiral waveform has a low frequency, low amplitude.**
- ▶ While they get closer, **frequency and amplitude increase up to the merging.**
- ▶ The final **remnant relax during ringdown**, when the wave is dumped.

[LVC, arXiv:1602.03837](#)



GW analysis with matched filtering

- ▶ Due to the low amplitude of the signal from binary systems, the analysis of the GW rely on **matched filtering** to evaluate the correlation between the signal template h and the data s

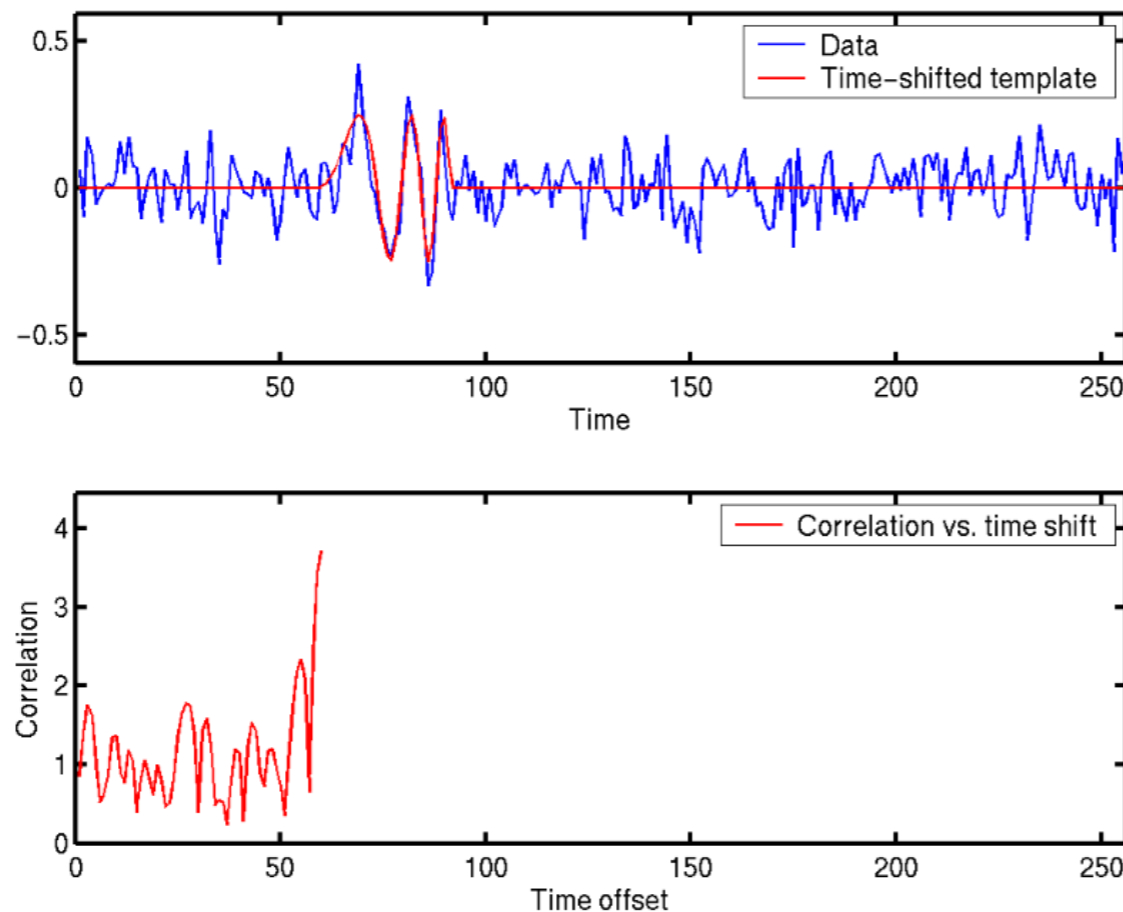


Source: L. Candonati

$$z(t) = 4 \int h^*(f) s(f) \exp(2\pi i f t) df$$

GW analysis with matched filtering

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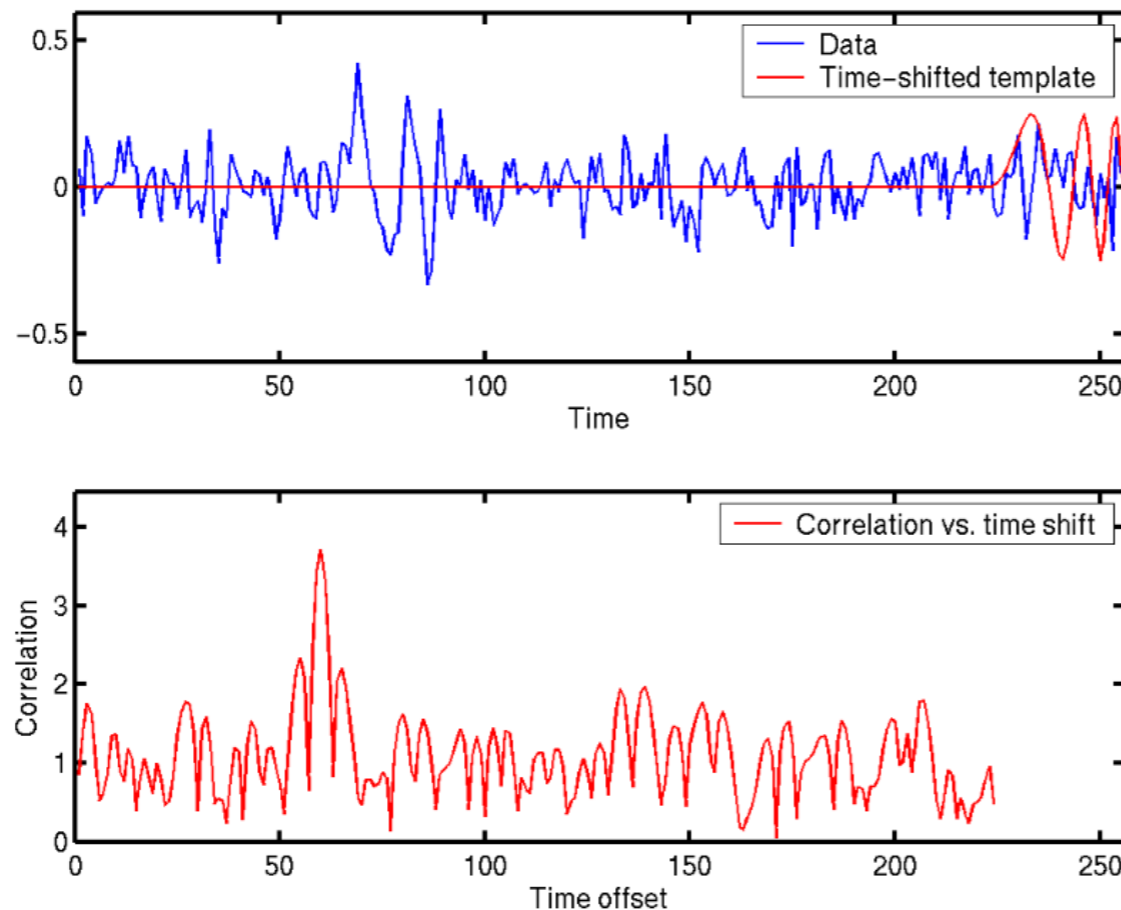


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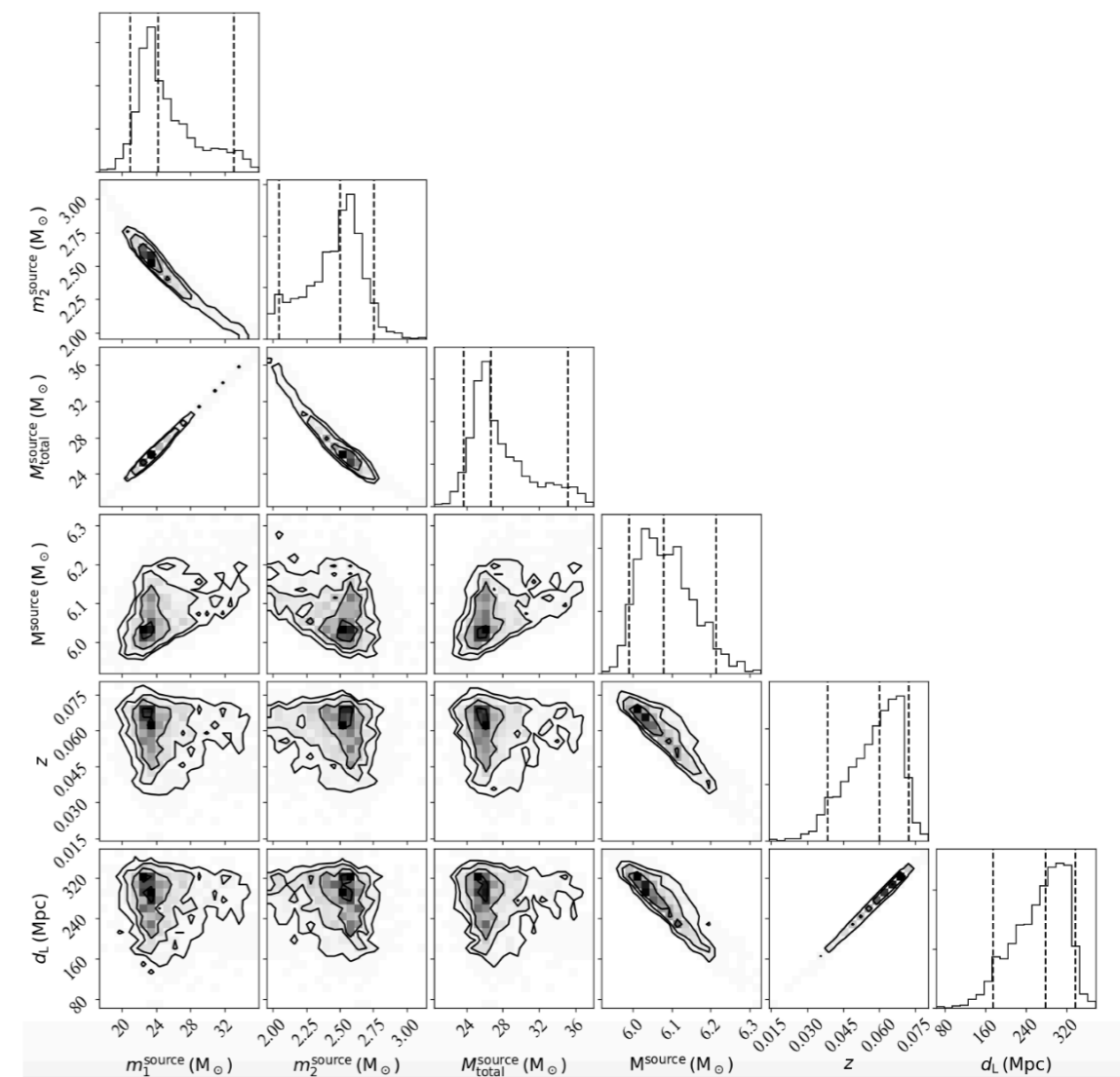


Source: L. Candonati

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GW parameter estimation

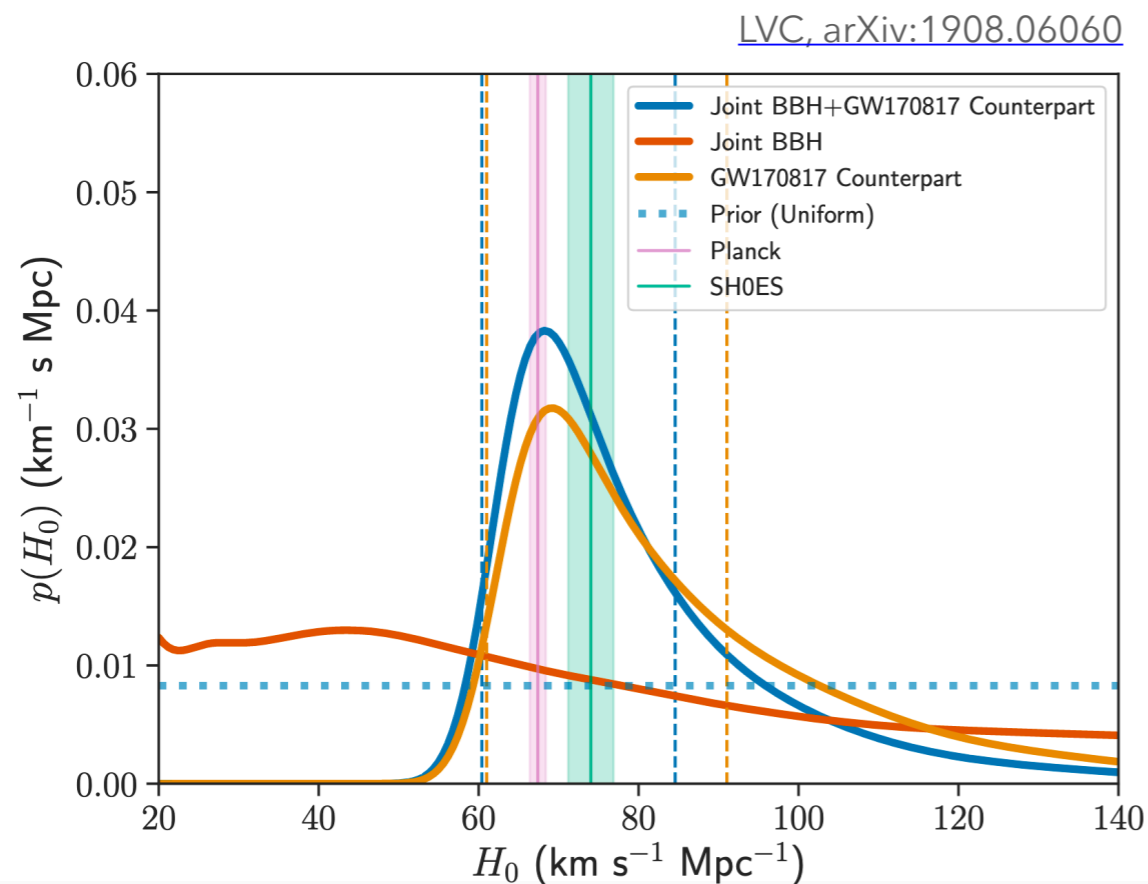
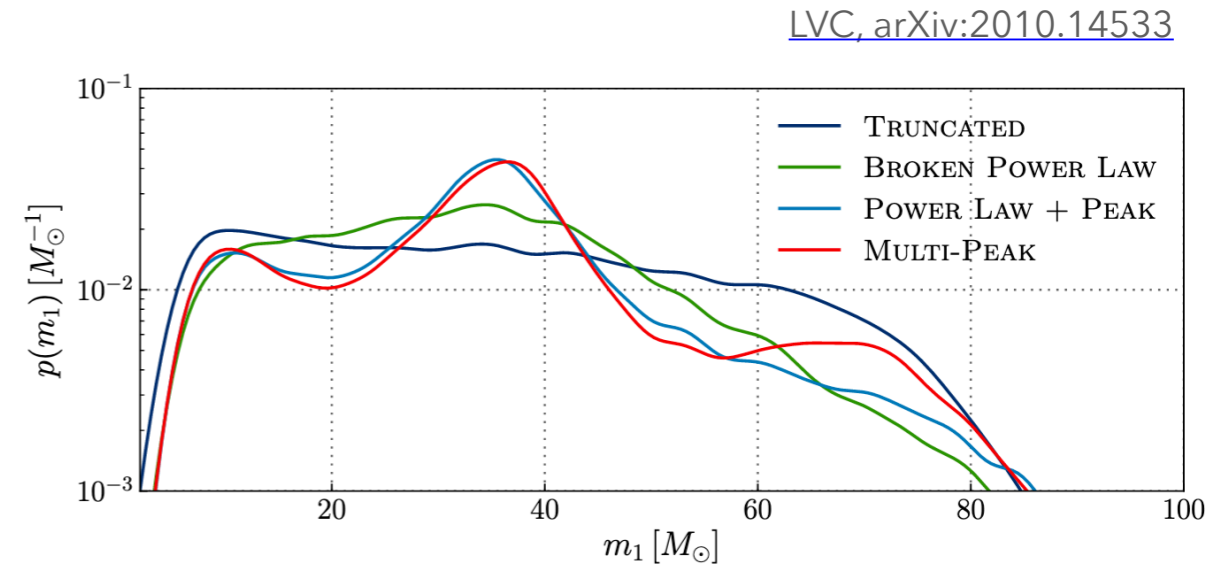
- ▶ The posterior probabilities of the parameters of the source are estimated with **Markov chains sampling methods** (Nested sampling, MCMC).
- ▶ **15 parameters minimum** to describe a binary system:
 - 2 masses
 - 2 spin magnitudes
 - 2 angles for each spin
 - Reference time
 - Orbital phase at reference time
 - Luminosity distance
 - Right ascension & declination
 - Inclination angle
 - Polarisation angle



GW physics

- A primer on GW astrophysics
- Ground-based interferometers
- Detection and analysis
- **Examples of physics results**

- ▶ **Astrophysical distribution:** presence of features compare to the star power-law distribution

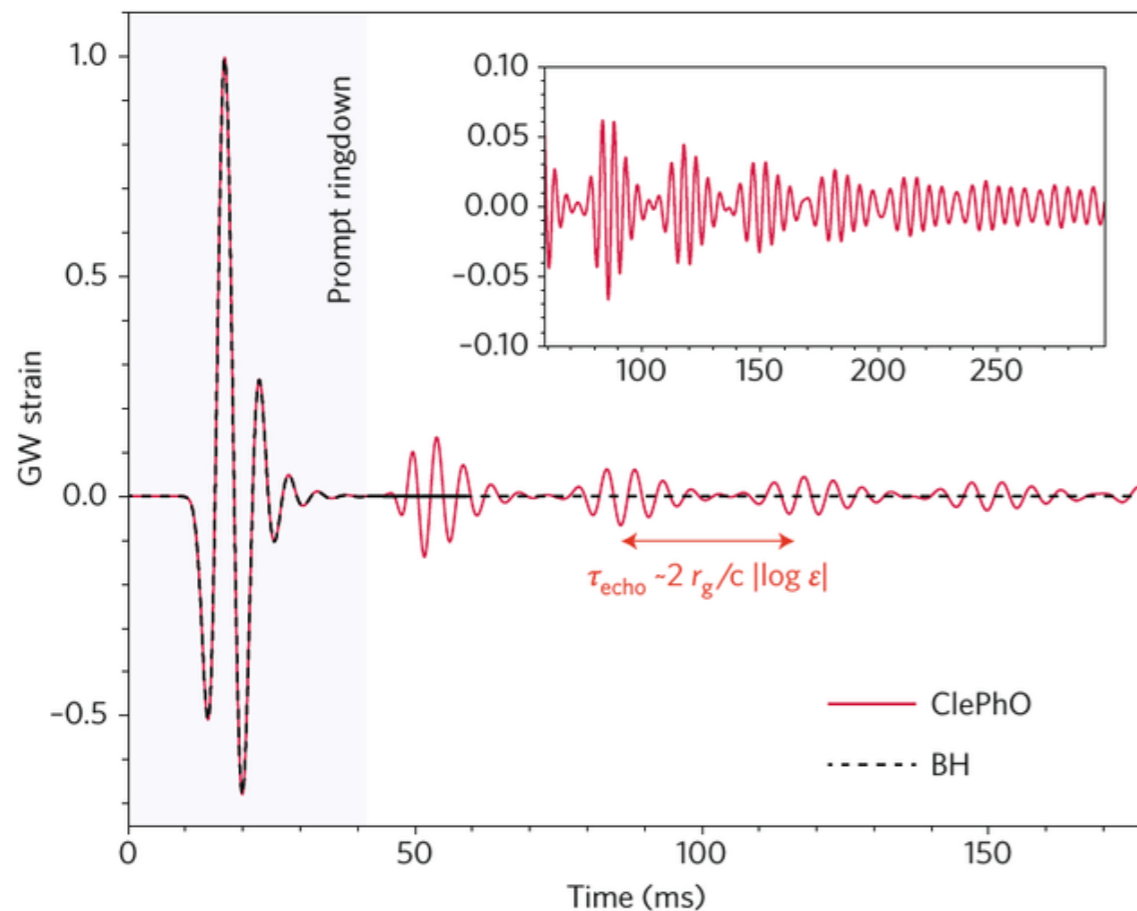


- ▶ **Neutron stars binary:** the presence of an electromagnetic counterpart enables to measure the Hubble constant

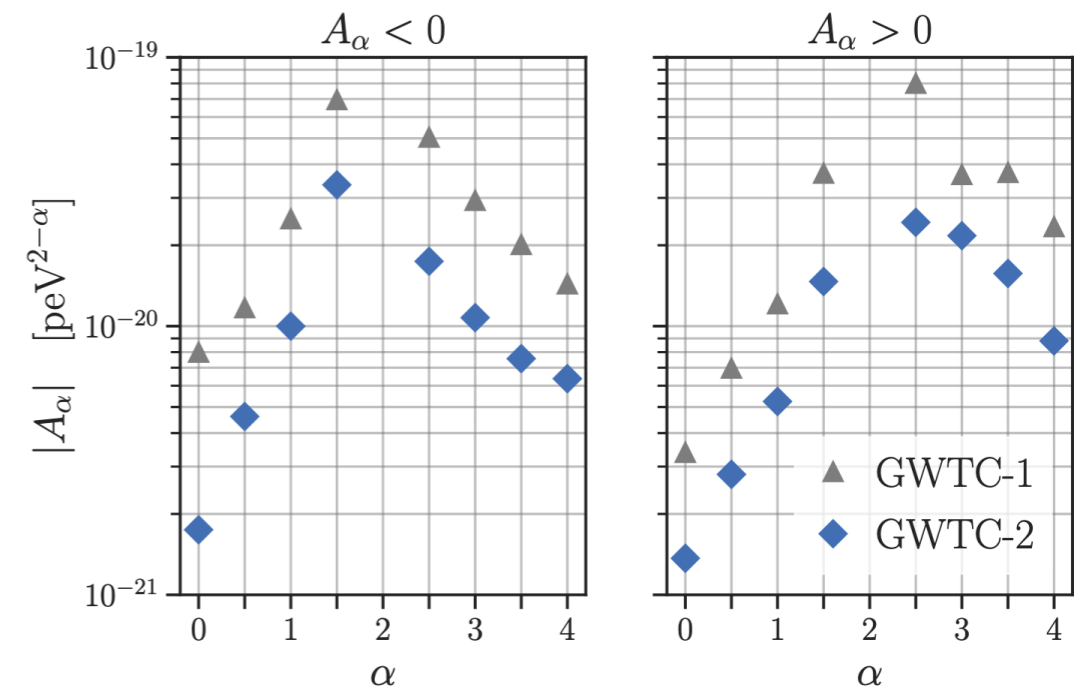
GW fundamental physics

- ▶ **GW propagation:** constraints on the mass of the graviton and other alternative theories of gravitation

[Cardoso & Pani, arxiv:1709.01525](#)



[LVC, arXiv:2010.14529](#)



- ▶ **GW ringdown (end of signal):** the presence of higher harmonics or echoes can help testing the nature of the black holes as sources of GW

Machine learning applications

- **Why ML?**
- Characterisation of detector noise
- Detection of astrophysical signals
- GW modelling
- Estimation of the GW sources parameters

Machine learning usefulness

- ▶ **Small signals:** the amplitude of the signal is \sim the amplitude of the noise
- ▶ **Complex system:** the Einstein Equations are non-linear and the physics of the strong-field regime is highly complex
- ▶ **High dimensionality:** from the detectors channels to the binary characterisation, the systems need many parameters to be described
- ▶ **Computationally intensive:** solving Einstein Equations require numerical relativity simulations on superclusters, sampling the source parameters probabilities can take weeks with distributed computing
- ▶ **Review article:** Enhancing Gravitational-Wave Science with Machine Learning, [Machine Learning: Science and Technology, arXiv:2005.03745](https://arxiv.org/abs/2005.03745)

Machine learning applications

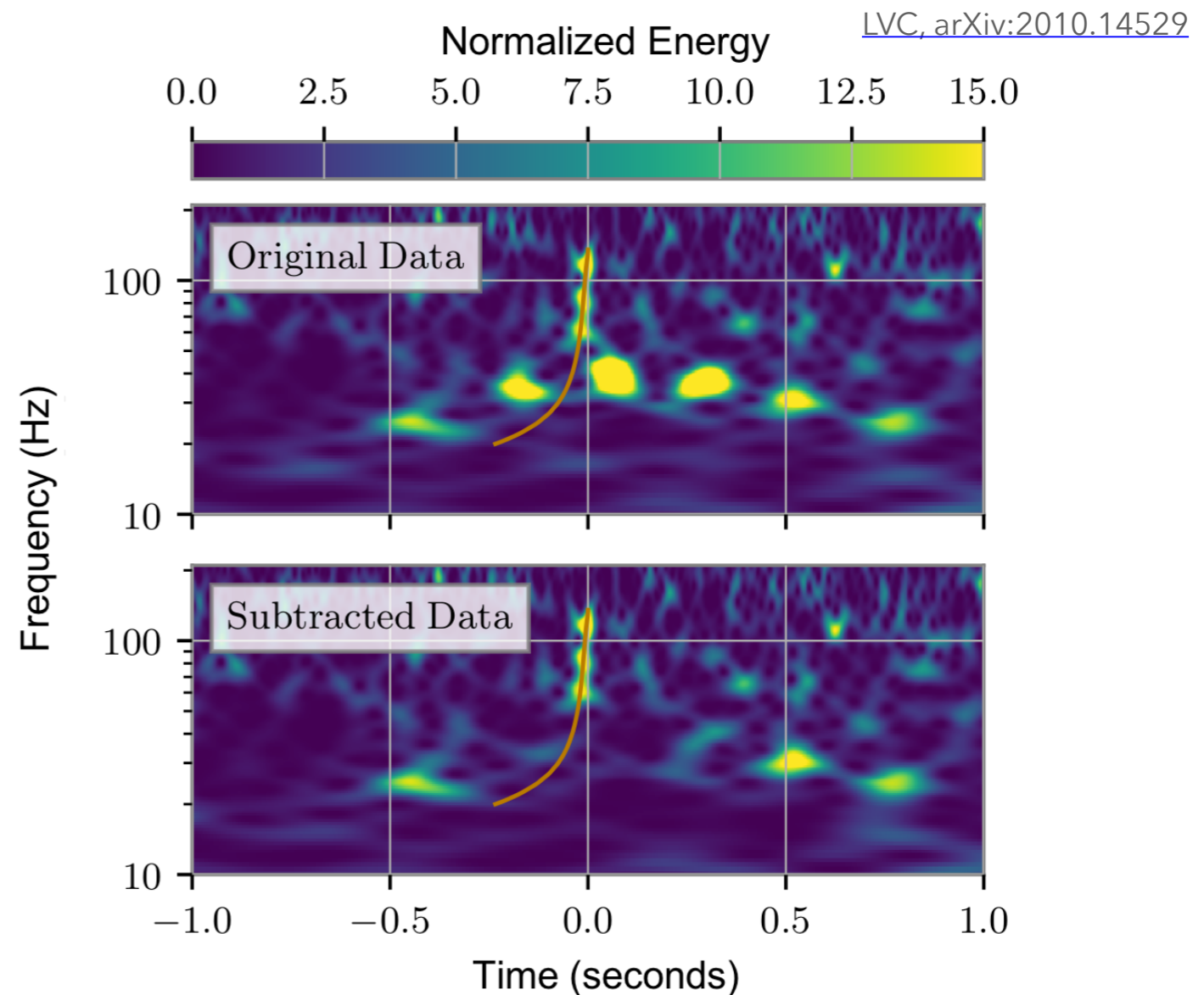
- Why ML?
- **Characterisation of detector noise**
- Detection of astrophysical signals
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Detector glitches

- ▶ **Glitches:** Short-lived non-stationary and nonlinear transients signals of environmental / instrumental origin

- ▶ **Characterisation:**

- Origin needs to be understood to understand the noise of the detectors
- Glitches can occur at the same time than signals and need to be subtracted
- Several different morphologies

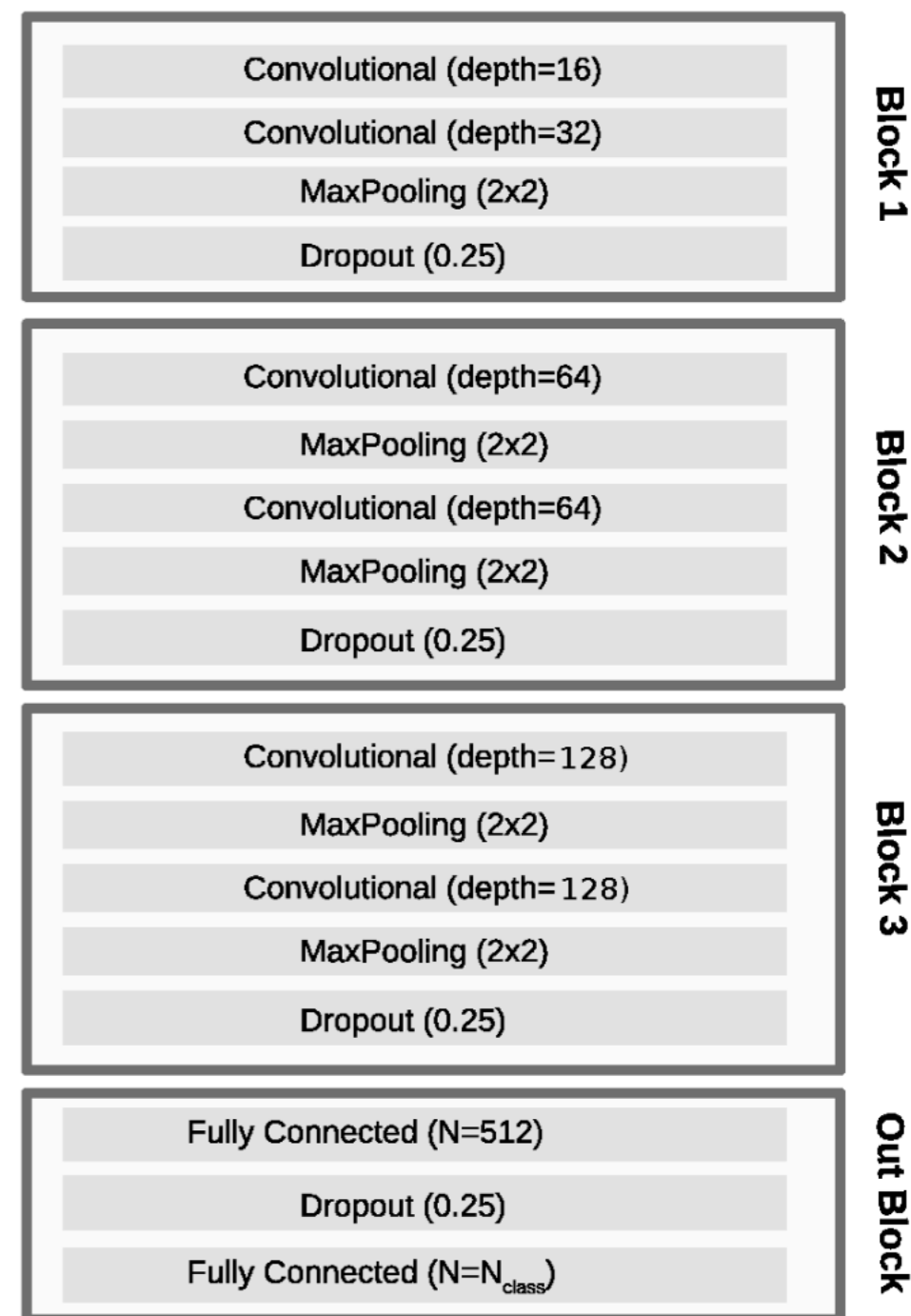


Characterisation of glitches with CNN

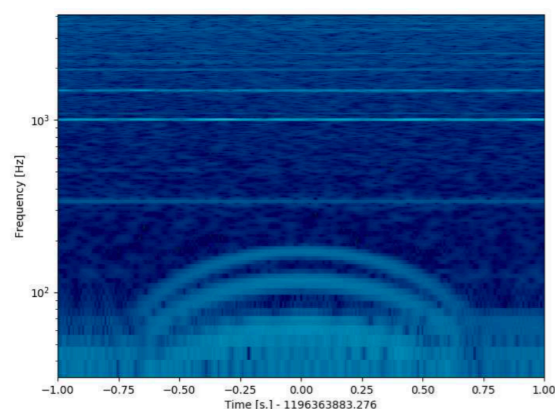
▶ **Spectrograms:** time/frequency maps provides 2D representation of glitches analogous to images

▶ **Convolutional Neural Networks:**

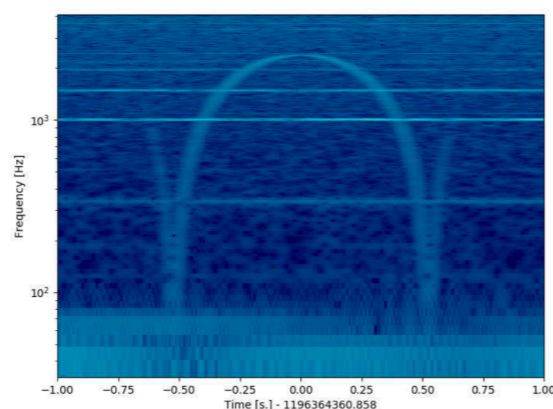
- CNN on simulated glitches offer 99% classification efficiency
- Supervised learning where categories are based on morphological features



[Razzano & Cuoco, arXiv:1803.09933](https://arxiv.org/abs/1803.09933)



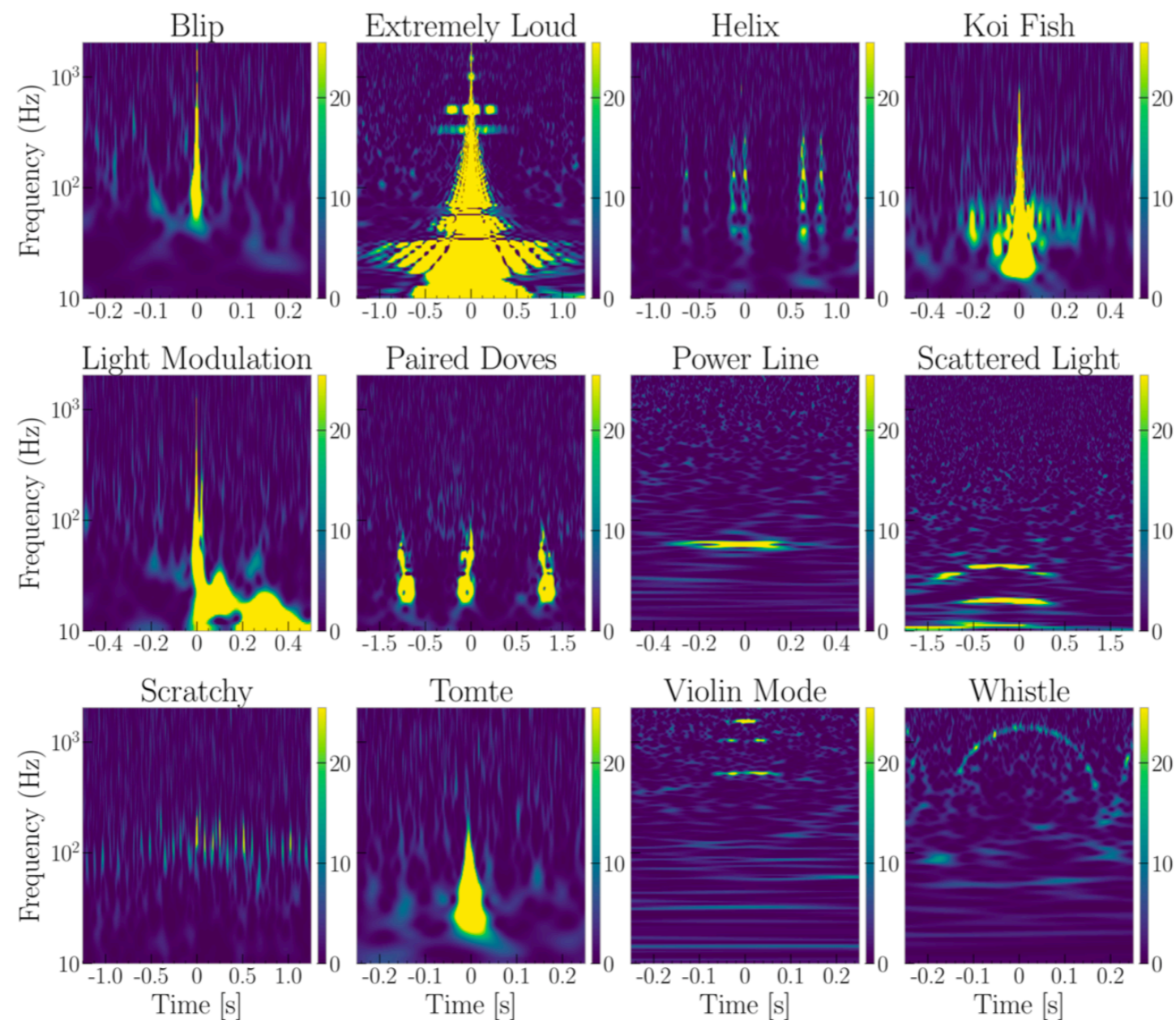
(e)



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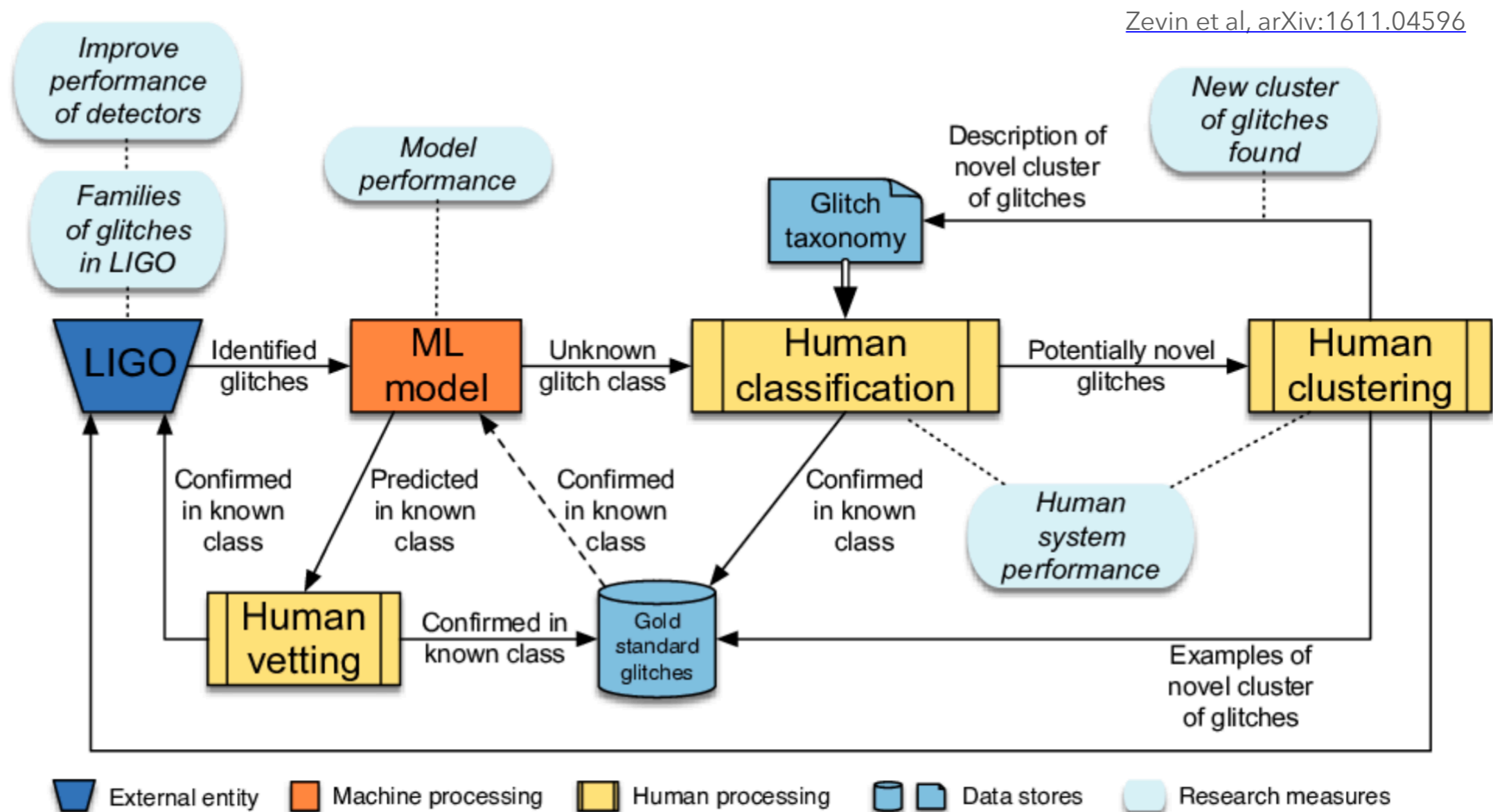
Human-based glitch tagging

- ▶ **GravitySpy**: citizen science project where anybody can tag glitches from LIGO and Virgo. Create a dataset for next ML application of glitch characterisation.



GravitySpy and machine learning

- ▶ **CNN efficiency:** training on citizen-tagged events show >0.9 correct tagging except for "Paired Doves" and "Wandering Lines" categories.

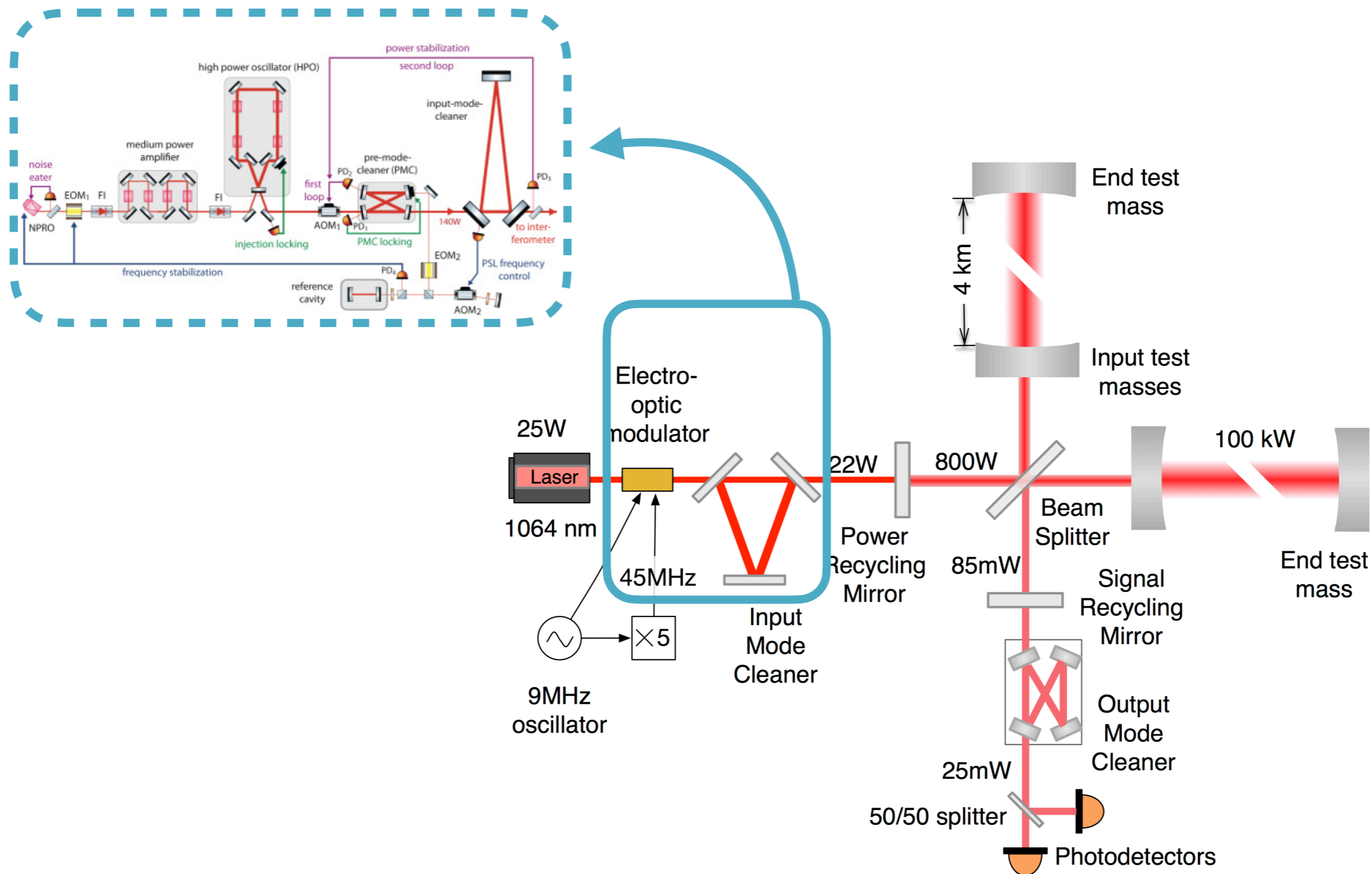


Machine learning applications

- Why ML?
- Characterisation of detector noise
- **Detection of astrophysical signals**
- GW modelling
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LIGO-Virgo auxiliary channels

- ▶ **Auxiliary channels:** a plethora of additional detectors monitoring the interferometers



[Kwee et al, Optics Express Vol. 20, Issue 10, pp. 10617-10634 \(2012\)](#)

[Martynov et al, arXiv:1604.00439](#)

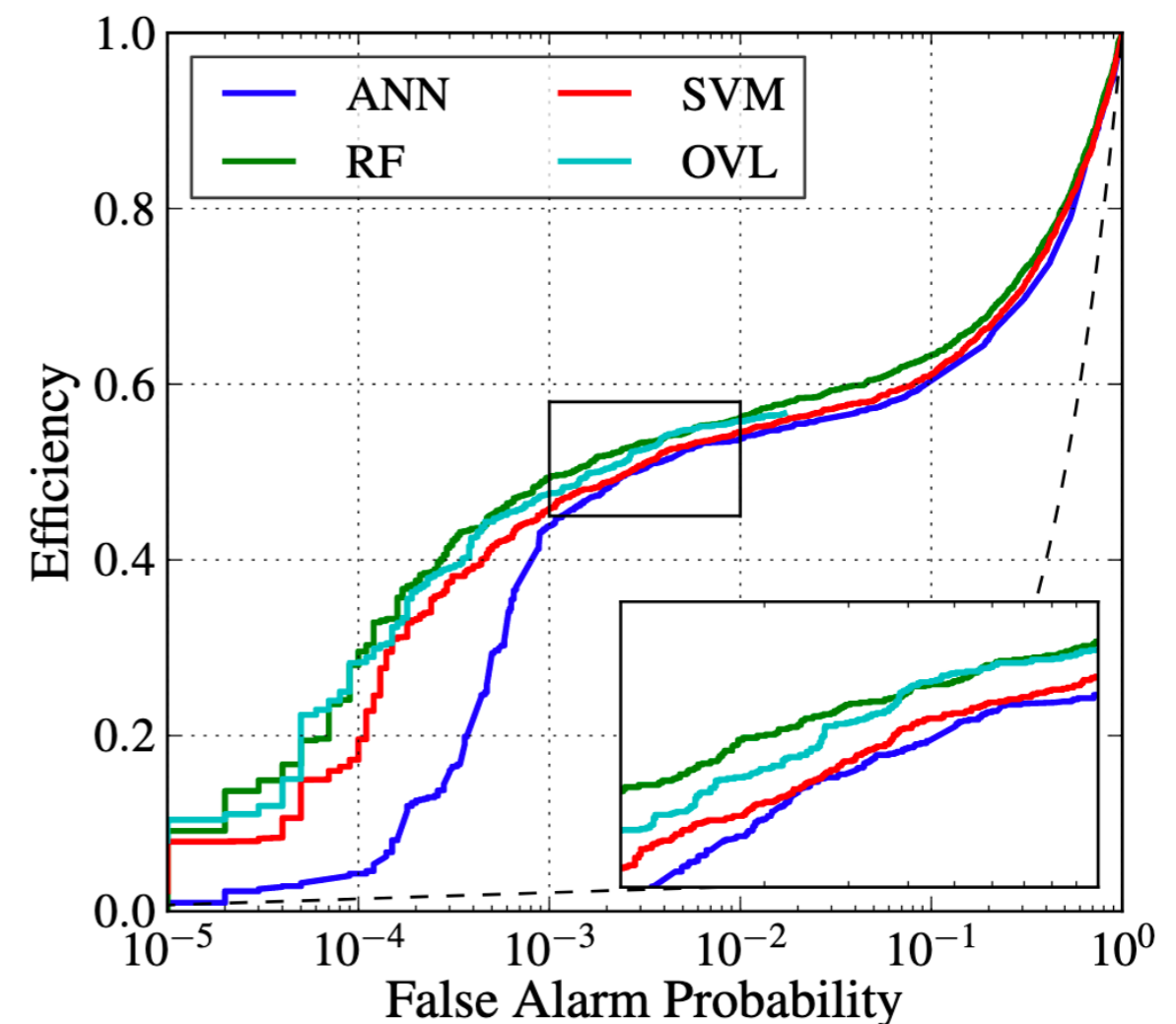
Identify astrophysical signals from noise

- ▶ **Glitches:** can be identified from astrophysical signals with the auxiliary channels

- ▶ **Comparison of ML algorithms:**

- Artificial Neural Network
- Support Vector Machines
- Random Forest
- Ordered Veto List
(correlation of glitches in GW / auxiliary channel with hierarchical ordering)

[Biswas et al, arXiv:1303.6984](#)

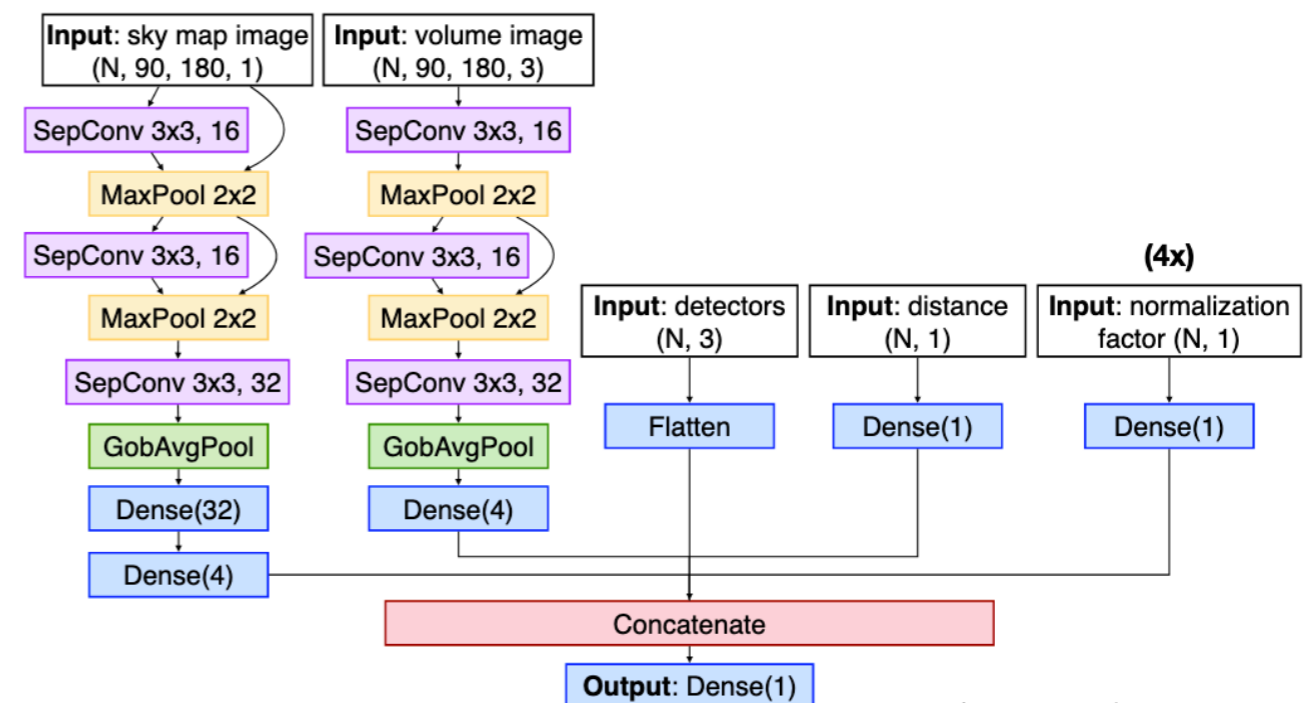
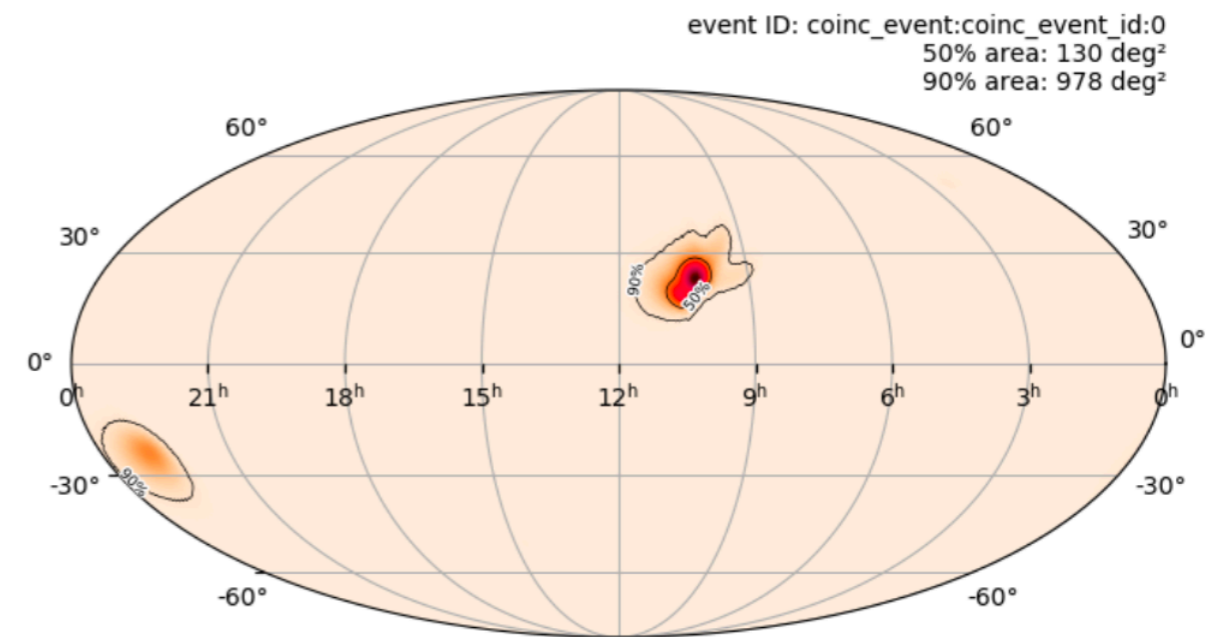


Using public data for electromagnetic alerts

- ▶ **Alerts:** are sent to multimessenger facilities when event false alarm rate is large. Can be retracted after further studies if the event is noise.

- ▶ **CNN classifiers:**

- Use public data only as inputs (sky localisation, distance, detector network)
- Correctly classify events from noise is 93% of cases
- Support the decision to follow GW events with telescopes



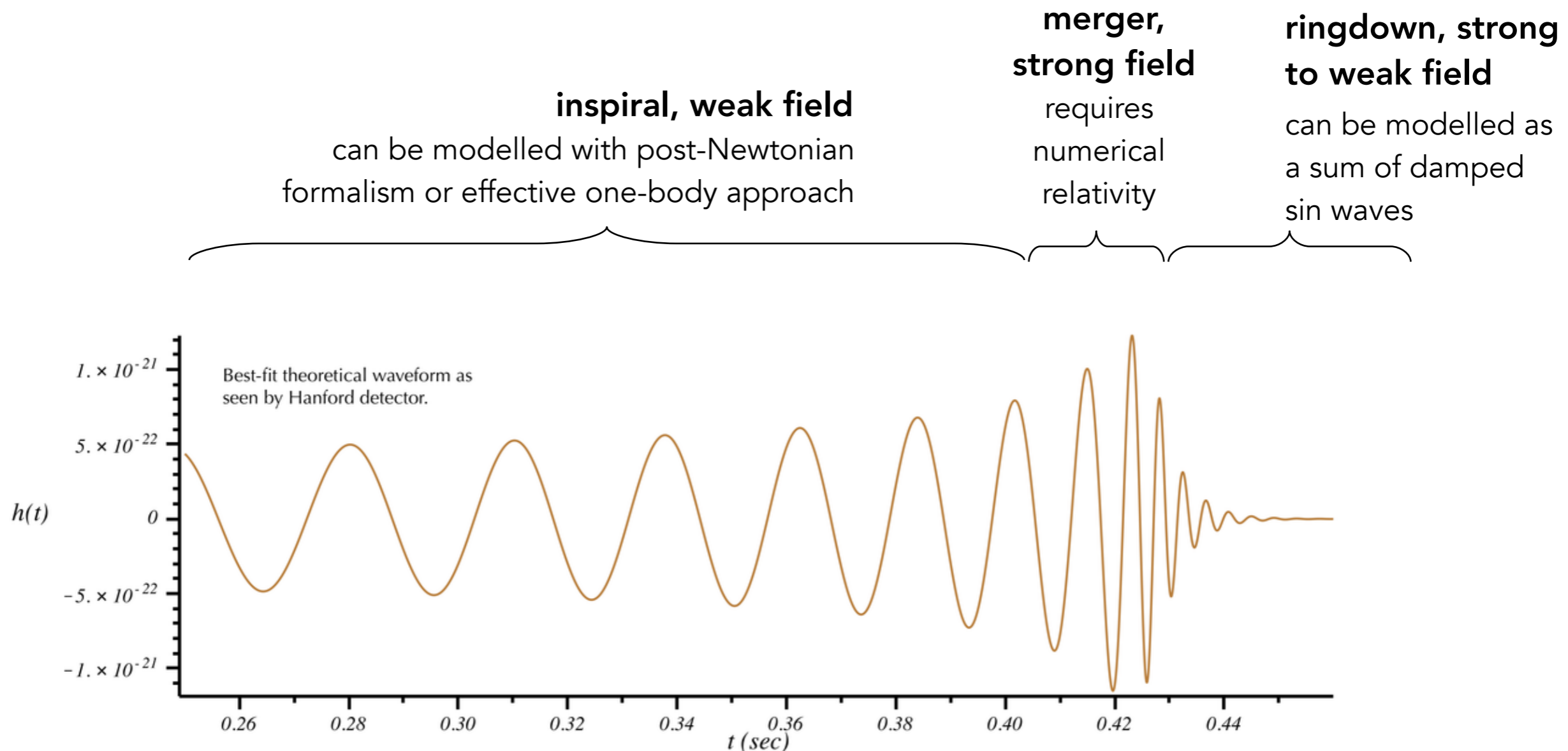
Cabero et al, 2010.11829

Machine learning applications

- Why ML?
- Characterisation of detector noise
- Detection of astrophysical signals
- **GW modelling**
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The necessity of GW modelling

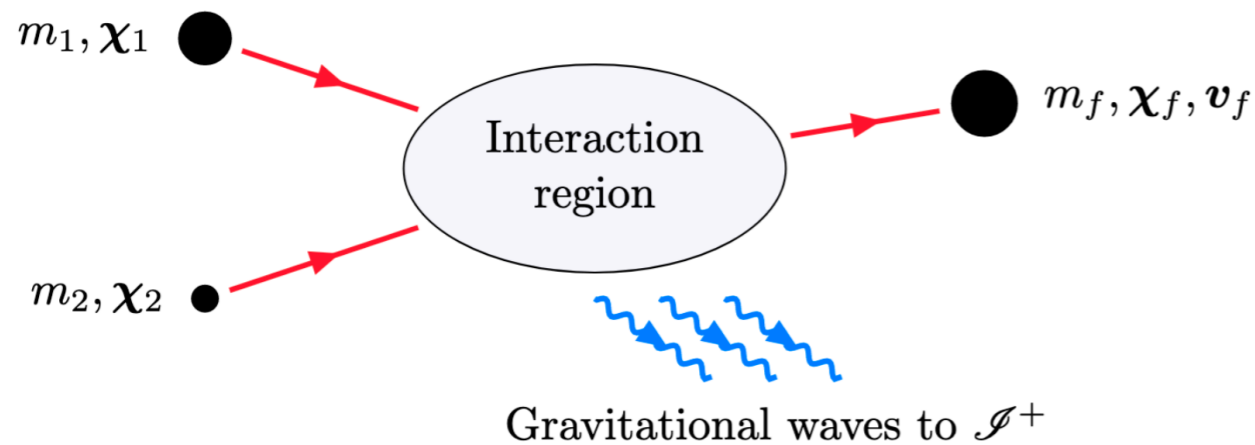
- ▶ **Necessity of a template bank of GW signals:** matched filtering algorithms and modelled search need to compare the data stream to templates
- ▶ **GW modelling:** approximate signals as numerical relativity simulations are too computationally intensive



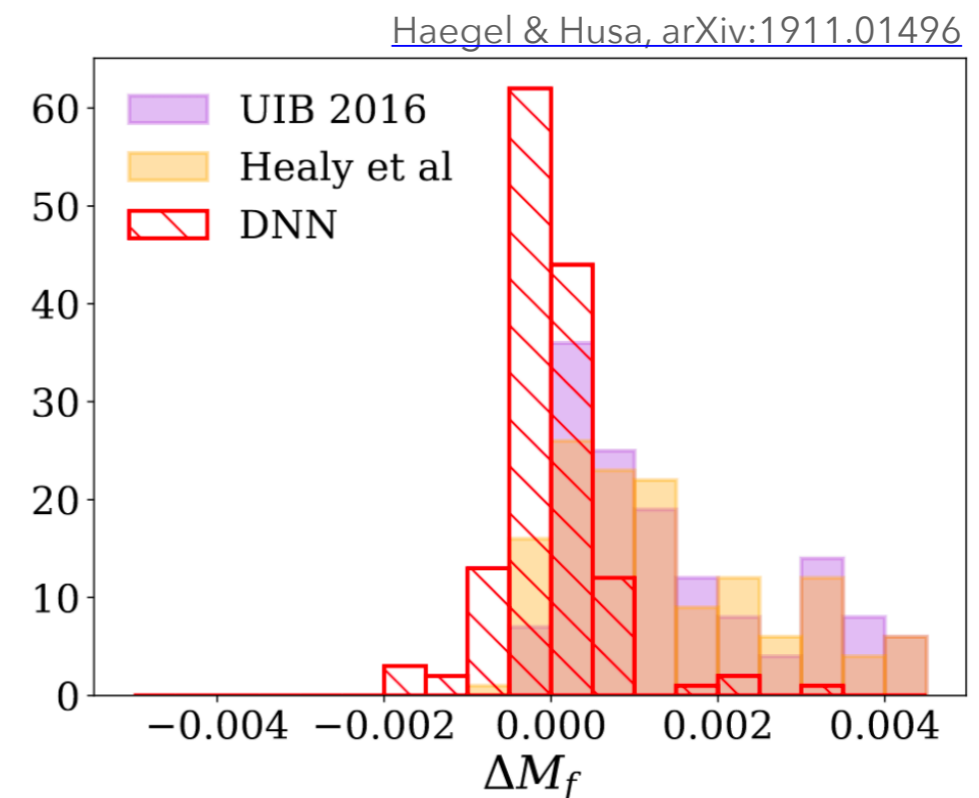
Source: Sound of Spacetime

Predicting the remnant parameters

- ▶ **Final black holes properties:** are important for GW modelling (final mass, spin)
- ▶ **Spinning black holes:** induce precession in the binary, high-dimensional (7 parameters) system to model, traditionally approximated
- ▶ **ML applications:** neural networks and GP can fully take into account the spin effects and correct biases in the prediction



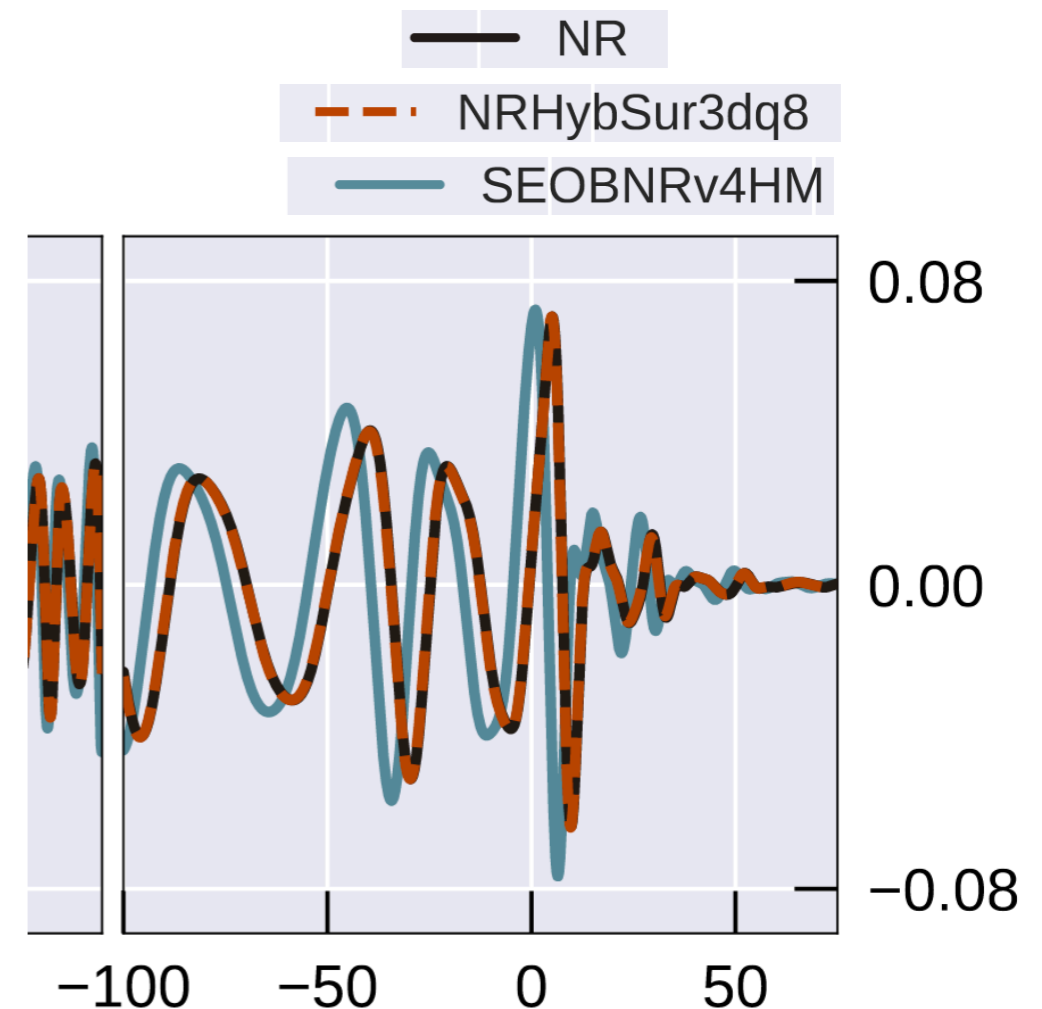
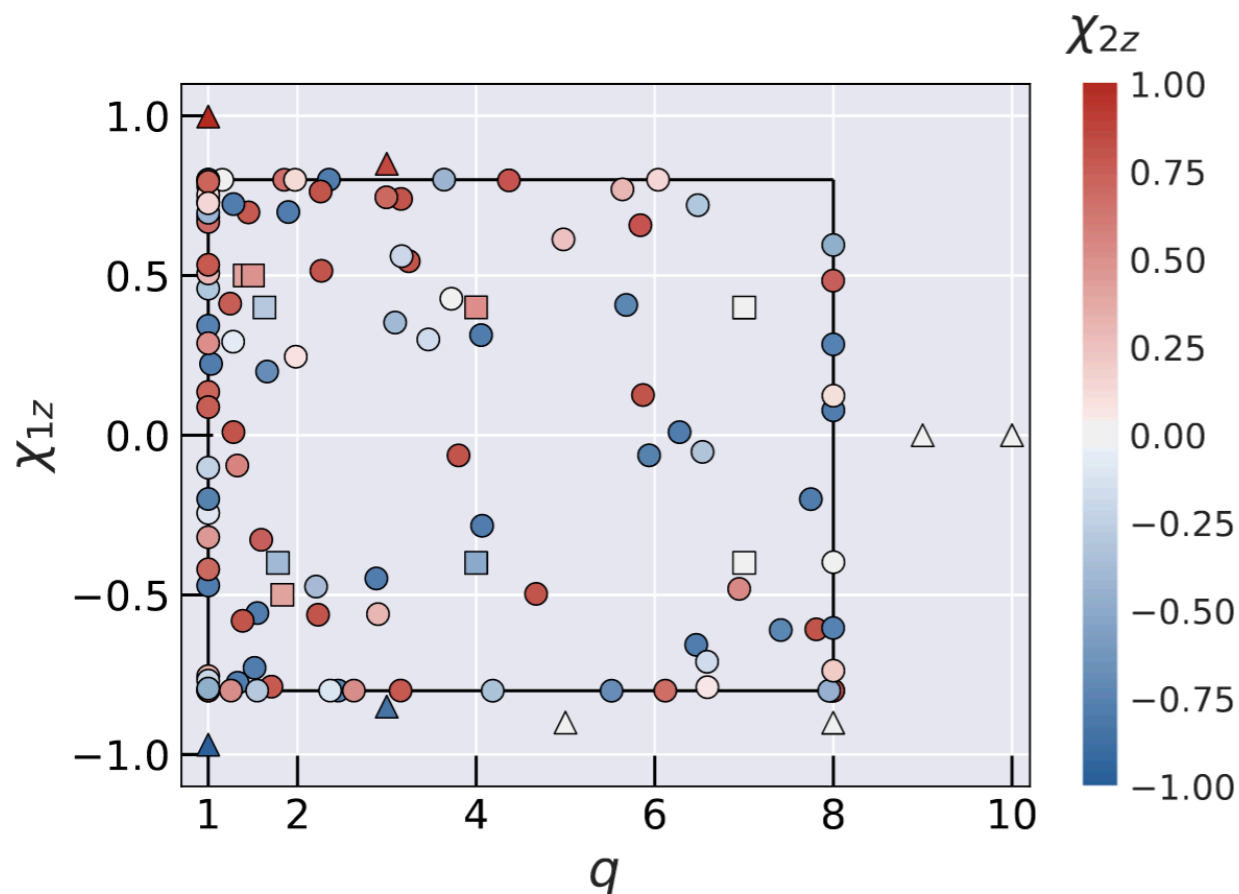
[Varma et al, arXiv:1809.09125](#)



Interpolating numerical relativity simulations

- ▶ **Gaussian Process:** can be trained on numerical simulations to generate GW template
- ▶ **Interpolation:** in the parameter space of the simulations
- ▶ **Errors:** of the GP training can be naturally propagated into parameter inference

[Varma et al, arXiv:1809.09125](#)

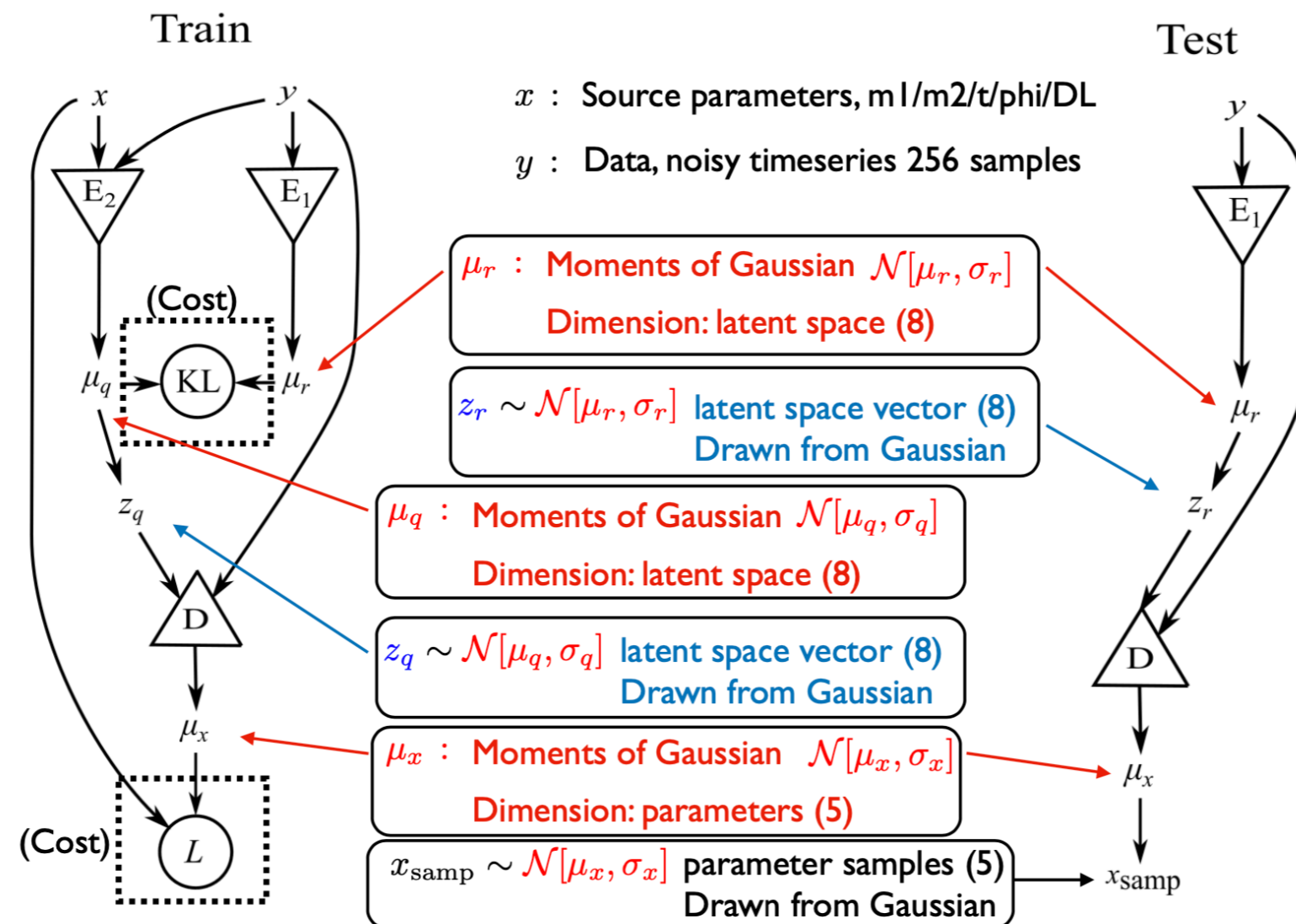


Machine learning applications

- Why ML?
- Characterisation of detector noise
- Detection of astrophysical signals
- GW modelling
- **Estimation of the GW sources parameters**

Estimation of GW source parameters

- ▶ **Markov chain sampling:** slow process (up to weeks)
- ▶ **Conditional variational auto-encoder (CVAE):** minimize the cross-entropy between the true Bayesian posterior and an approximate Bayesian posterior produced by the neural network



Sylvain Marsat — APC

5

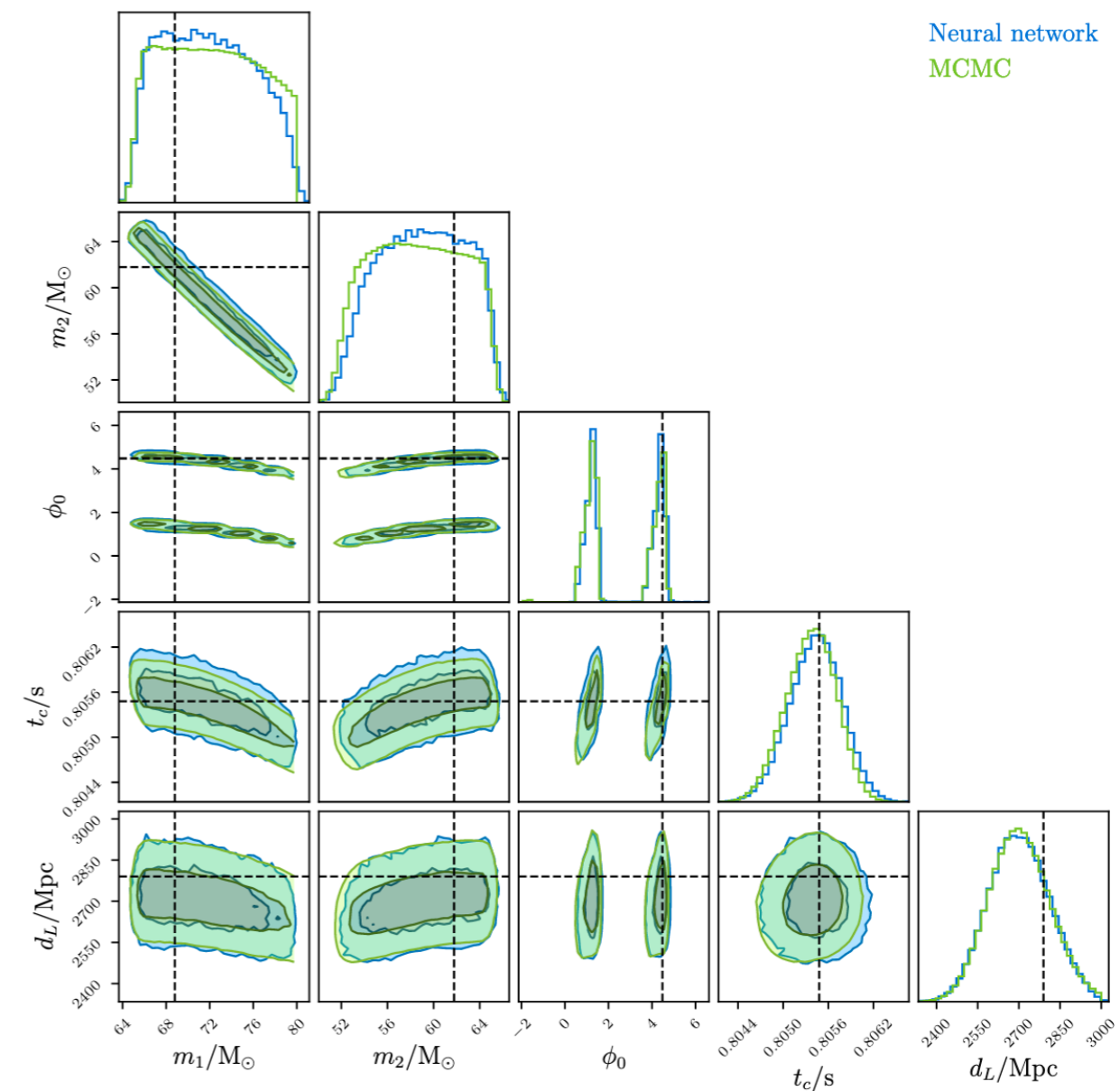
APC — Paris — 2019-02-03

[Gabbard et al, arXiv:1909.06296](https://arxiv.org/abs/1909.06296)

Estimation of GW source parameters

- ▶ **Normalizing flow:** invertible transformations to transform a simple initial distribution (multivariate Gaussian) into a more complex target distribution (posterior probability density of source parameters)

- ▶ **Quick estimate:** both methods provide estimates consistent with MCMC in a much reduced time (~ 1 mn)



(c) CVAE+

Thank you for your attention

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